

Stellar Evolution Modelling:

1D to 3D to 1D

(convection)

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in collaboration with:

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MESA: B. Paxton (KITP), F. X. Timmes, Arizona (US)

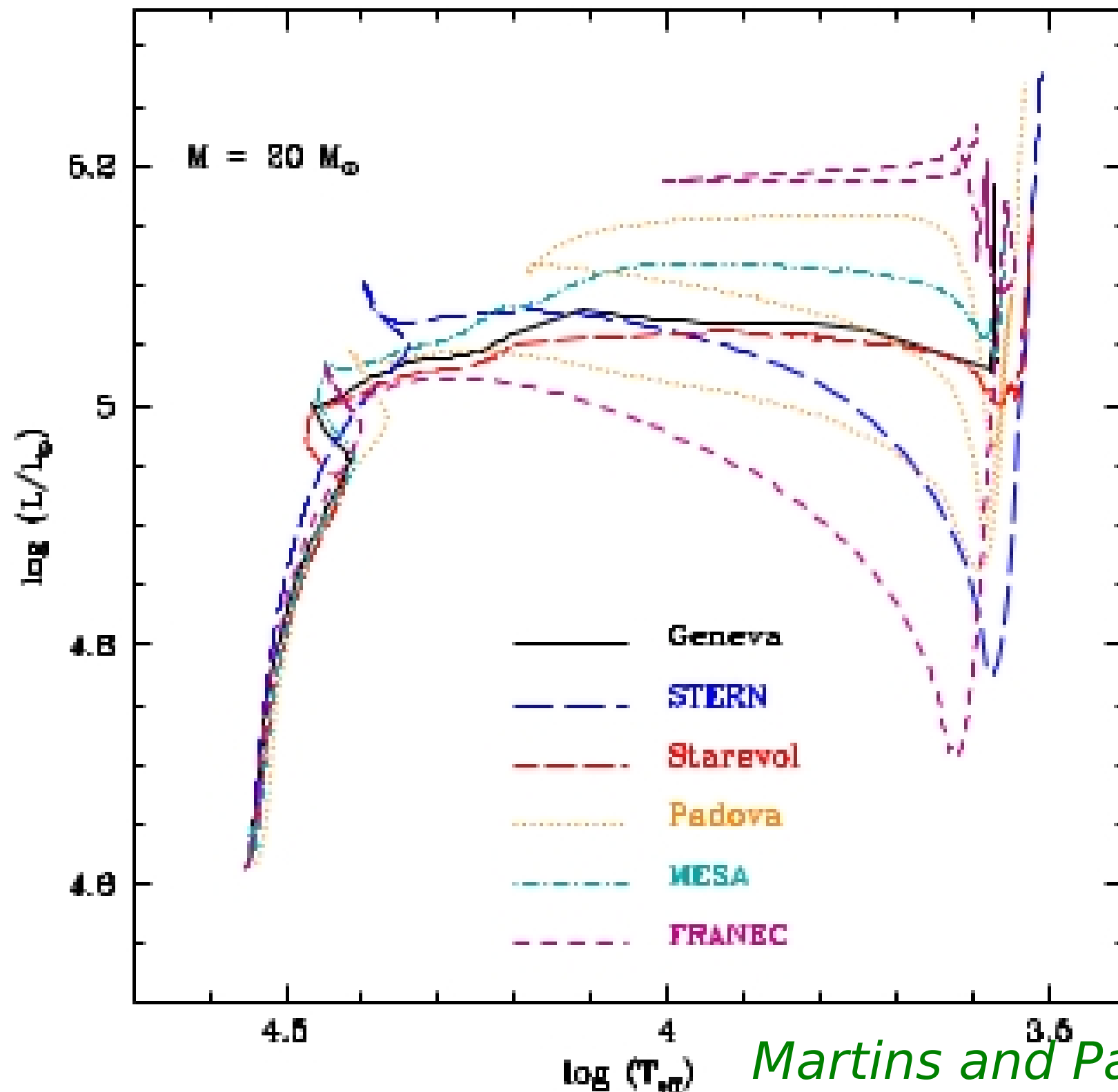
HYDRO: C. Meakin, D. Arnett (Arizona), M. Viallet, V. Prat (MPA)

SNe: K. Nomoto (IPMU, J), T. Fischer (TUD, D)

Nucleo: F.-K. Thielemann, U. Frischknecht, M. Pignatari (Basel, CH), T. Rauscher (Herts, UK)

NUGRID: F. Herwig, S. Jones (Victoria, Canada), C. Fryer (LANL), Laird (York), UChicago, UFrankfurt, ...

Convective Boundary Mixing (CBM) impact on post-MS



Different prescriptions for mixing, CBM and free parameters affects extent of MS and post-MS evolution.

Martins and Palacios (2013)

Advantages

- model entire evolution ($\Delta t \sim 10^3$ yrs)
- compare to observations
- progenitor models

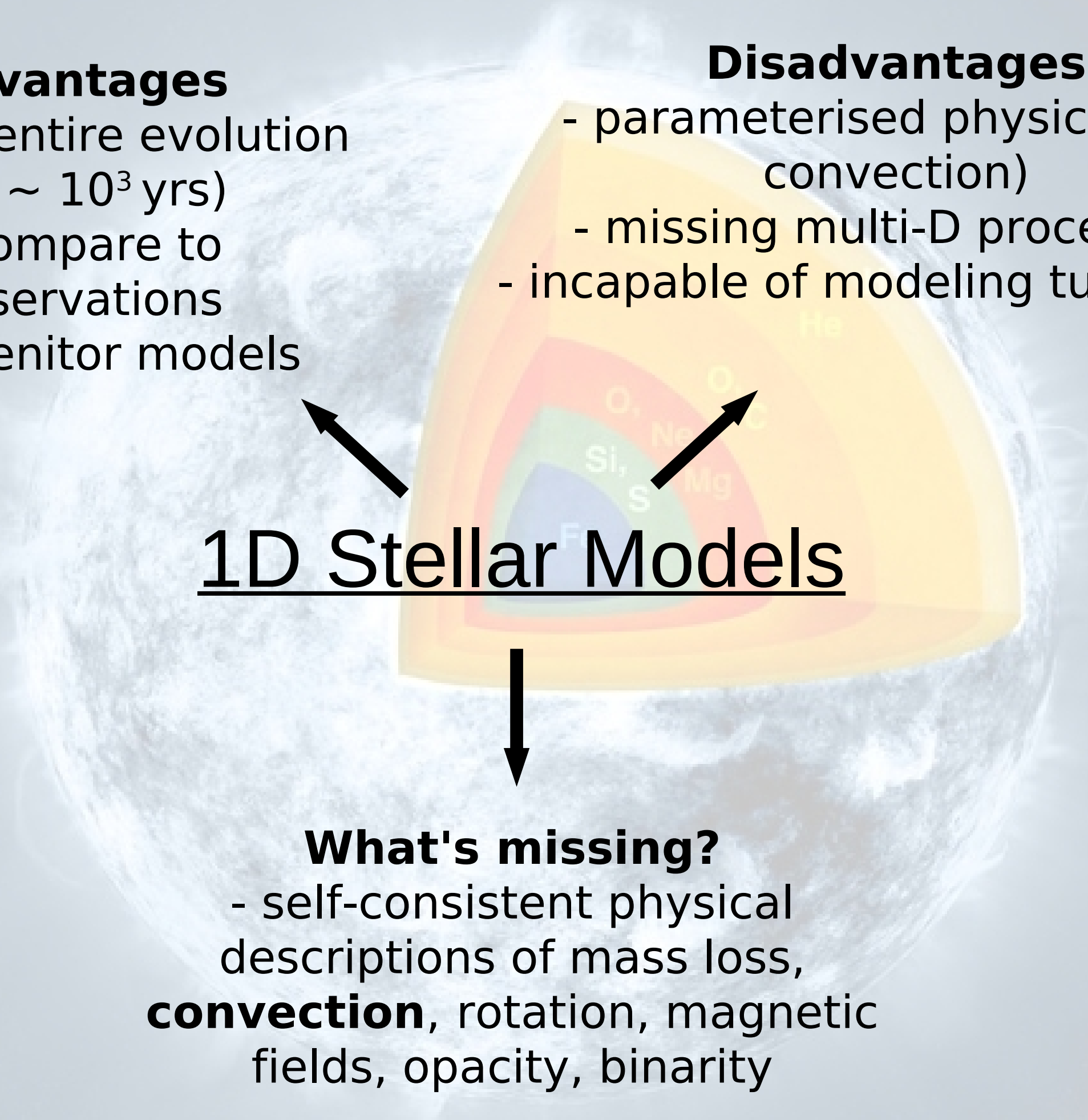
Disadvantages

- parameterised physics (e.g. convection)
- missing multi-D processes
- incapable of modeling turbulence

1D Stellar Models

What's missing?

- self-consistent physical descriptions of mass loss, **convection**, rotation, magnetic fields, opacity, binarity



Advantages

- model fluid instabilities (e.g. Rayleigh-Taylor)
- modeling 3D processes
- model diffusive and advective processes

Disadvantages

- resolution dependent?
- initial condition dependent?
- computational cost
- limited to dynamical timescales ($t_{\text{ct}} \sim 100\text{s}$)

3D Stellar Models

What's missing?

- full star simulations
- Large scale (LES) and small scale (DNS) cannot be followed simultaneously

Current Implementation: Convection

Multi-D processes

Major contributor to turbulent mixing

Turbulent entrainment at convective boundaries

Internal gravity waves

Bohm-Vitense (1958)

Mixing length theory,
boundary placement,
convective boundary mixing

1D prescriptions

Mixing rates

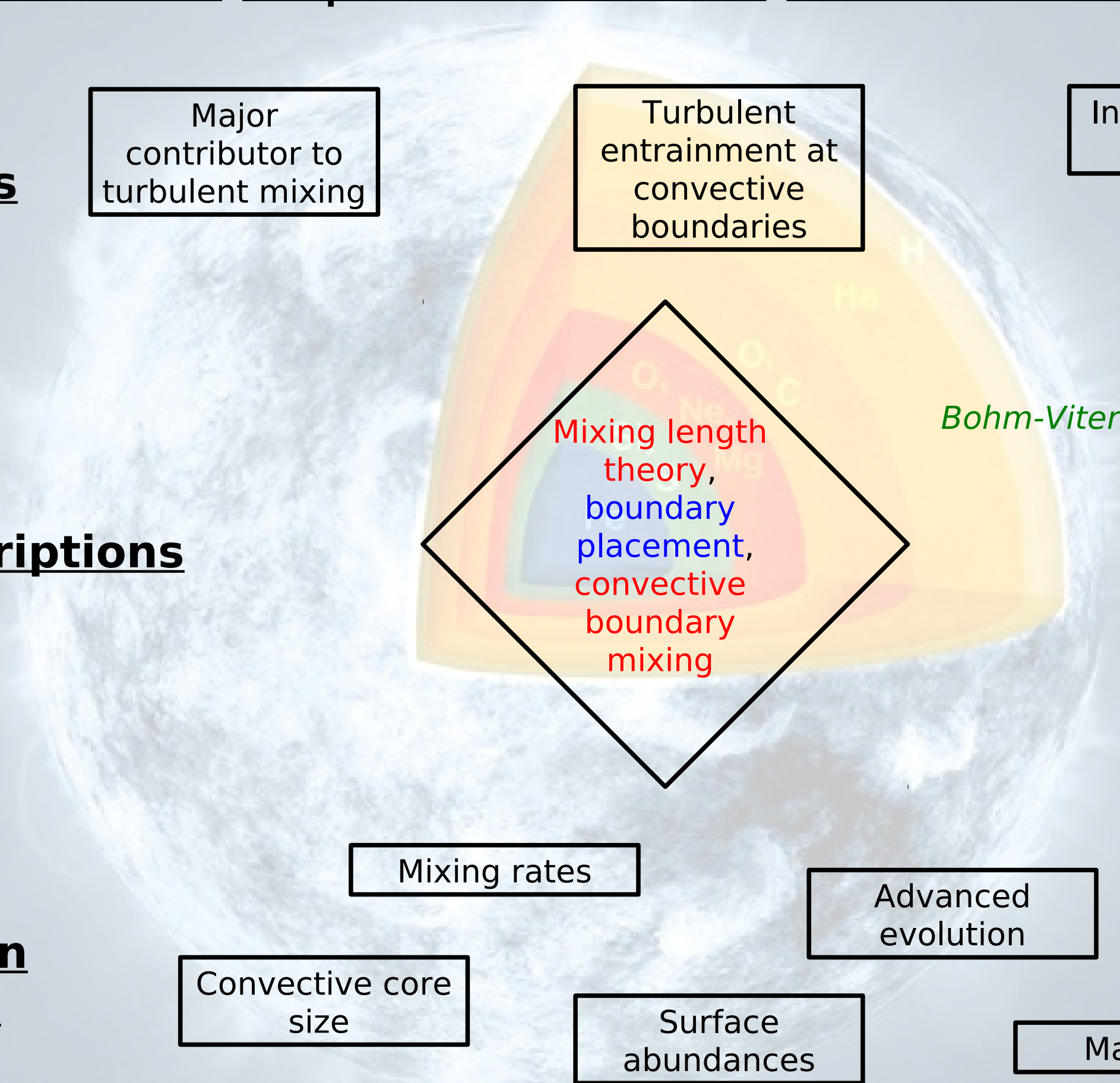
Advanced evolution

Impact on models

Convective core size

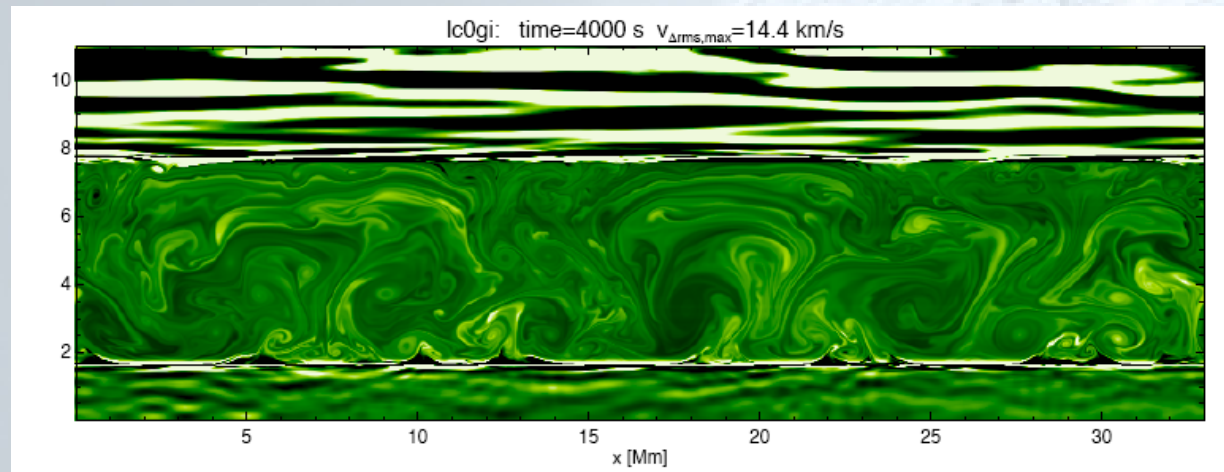
Surface abundances

Mass loss

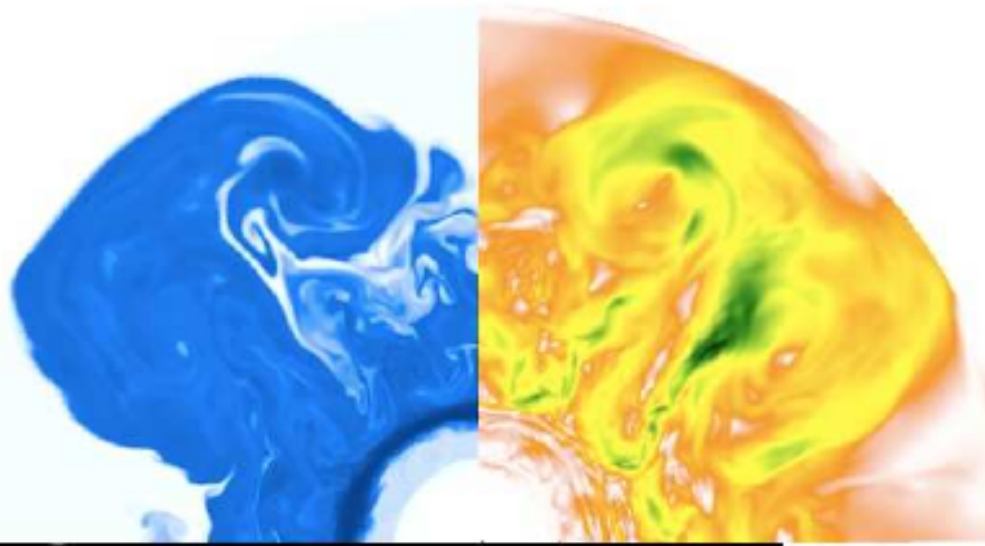


Way Forward

3D simulations

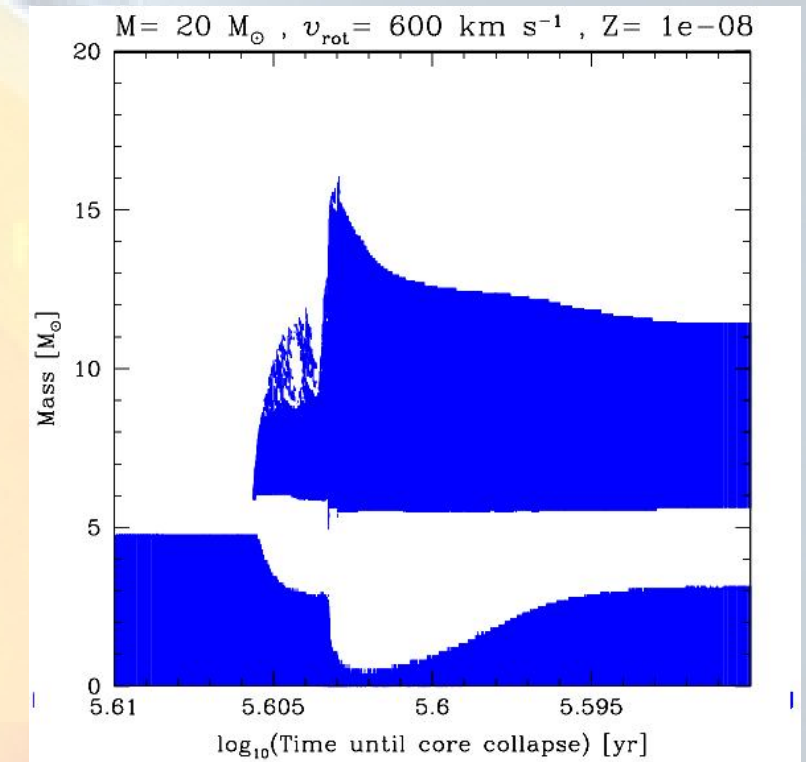


[Herwig et al 06](#)

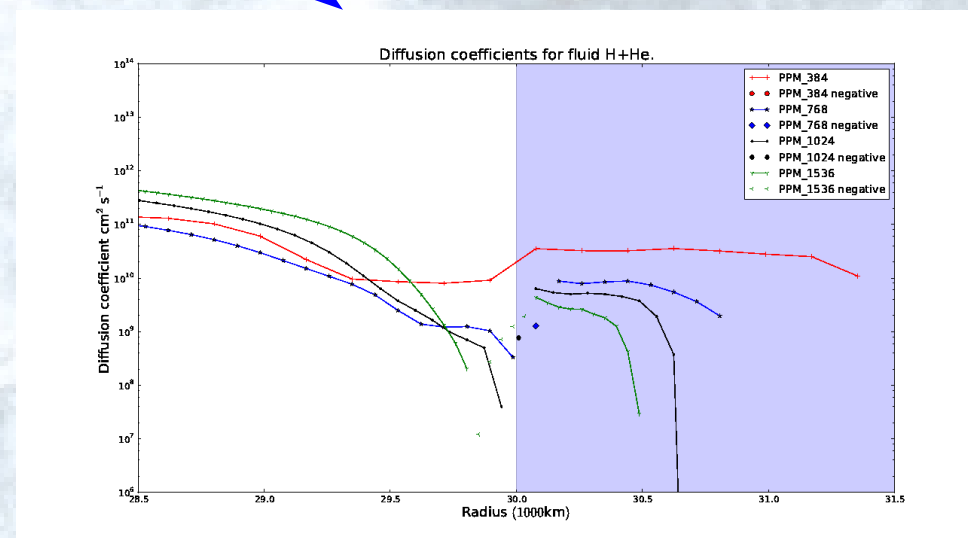


[e.g. Arnett & Meakin 2011](#)
[Mocak et al 2011,](#)
[Viallet et al 2013, ...](#)

Uncertainties in 1D



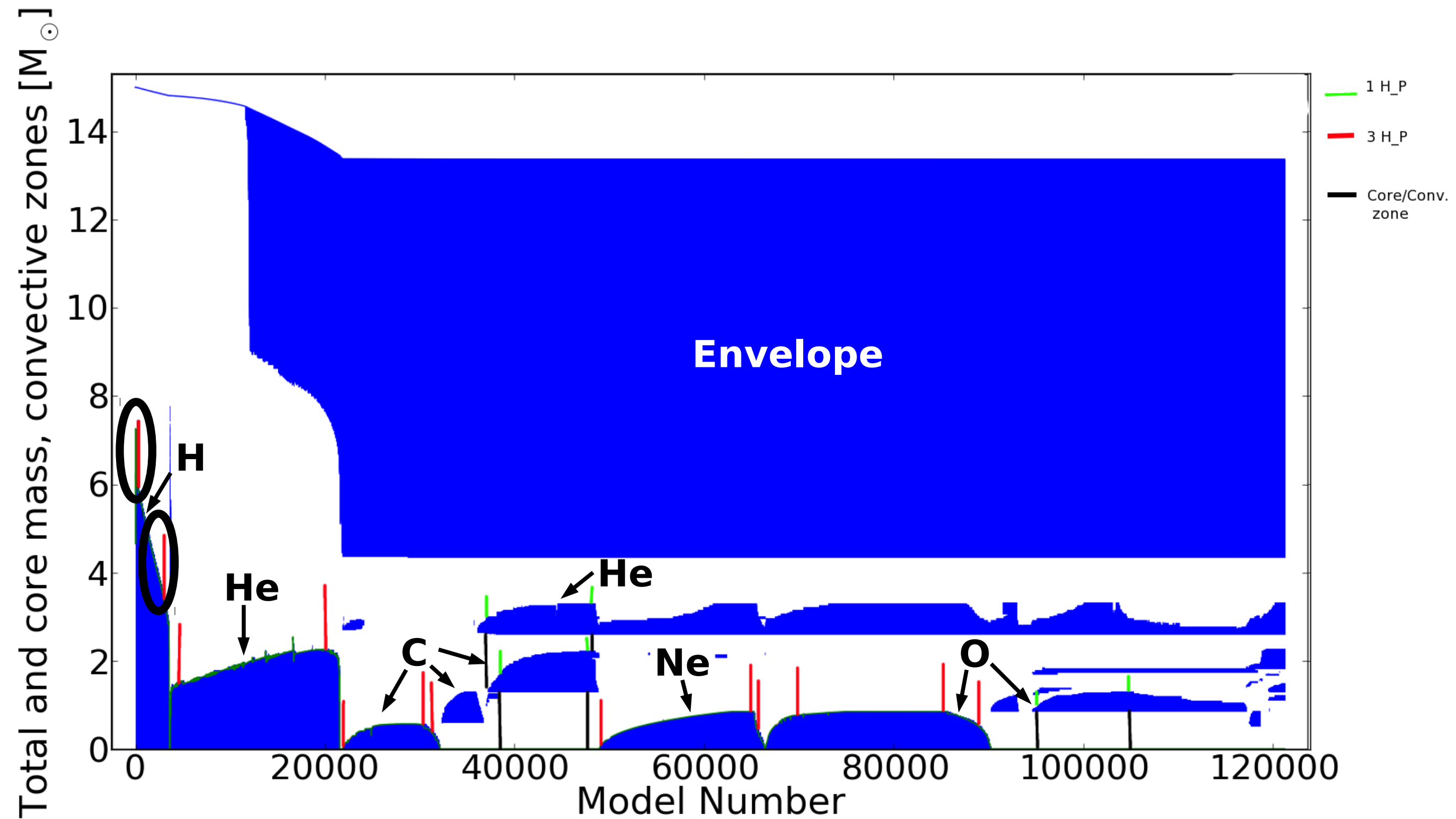
[e.g. Hirschi 07](#)



[Meakin et al 2009](#) ; [Bennett et al PhD thesis](#)

Determine effective diffusion (advection?) coefficient

Many Different Convective Zones in Stars!



1D to 3D: Priority List

* **Convective boundary mixing during core hydrogen burning:**

- + : many constraints (HRD, astero, ...)
- : difficult to model due to important thermal/radiative effects
- : long time-scale

* **Silicon burning:**

- + : important to determine impact on SNe of multi-D structure in progenitor (Couch & Ott, [aph1408.1399](#), Mueller & Janka [aph1409.4783](#))
- + : possible shell mergers occurring after core Si-burning (e.g. Tur et al [2009ApJ702.1068](#); Sukhbold & Woosley [2014ApJ783.105](#)) strongly affect core compactness
- + : radiative effects small/negl.
- : $\sim 10^9$ CPU hours needed for full silicon burning phase will be ok soon;
- : might be affected by convective shell history

* **AGB thermal pulses/H-ingestion:**

- + : already doable (e.g. Herwig et al [2014ApJ729.3](#), [2011ApJ727.89](#), Mocak et al [2010A&A520.114](#))
- + : thermal/radiative effects not dominant
- ? : applicable to other phases?

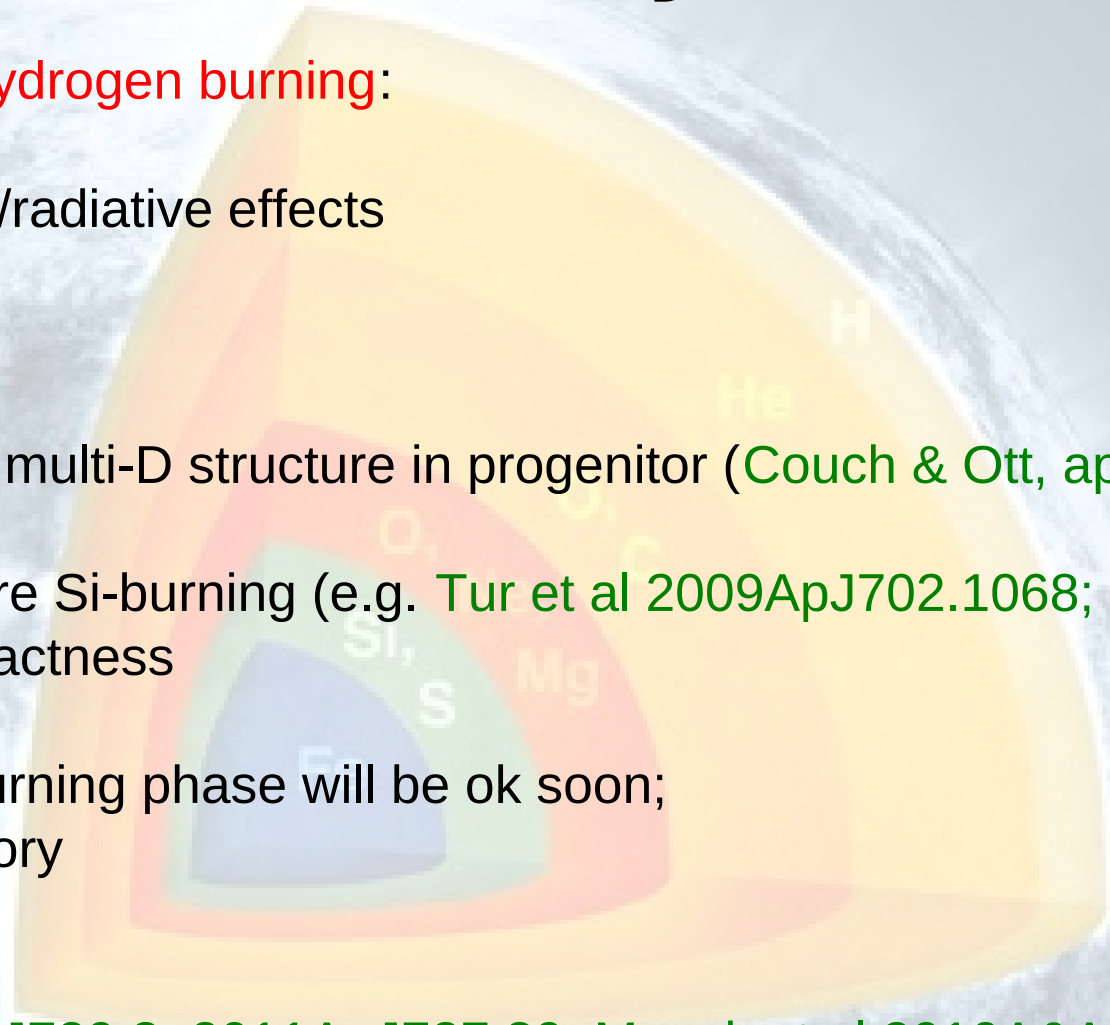
* **Oxygen shell:** (Meakin & Arnett [2007ApJ667.448/665.448](#), Viallet et al [2013ApJ769.1](#))

- + : similar to silicon burning but smaller reaction network needed
- : might be affected by convective shell history

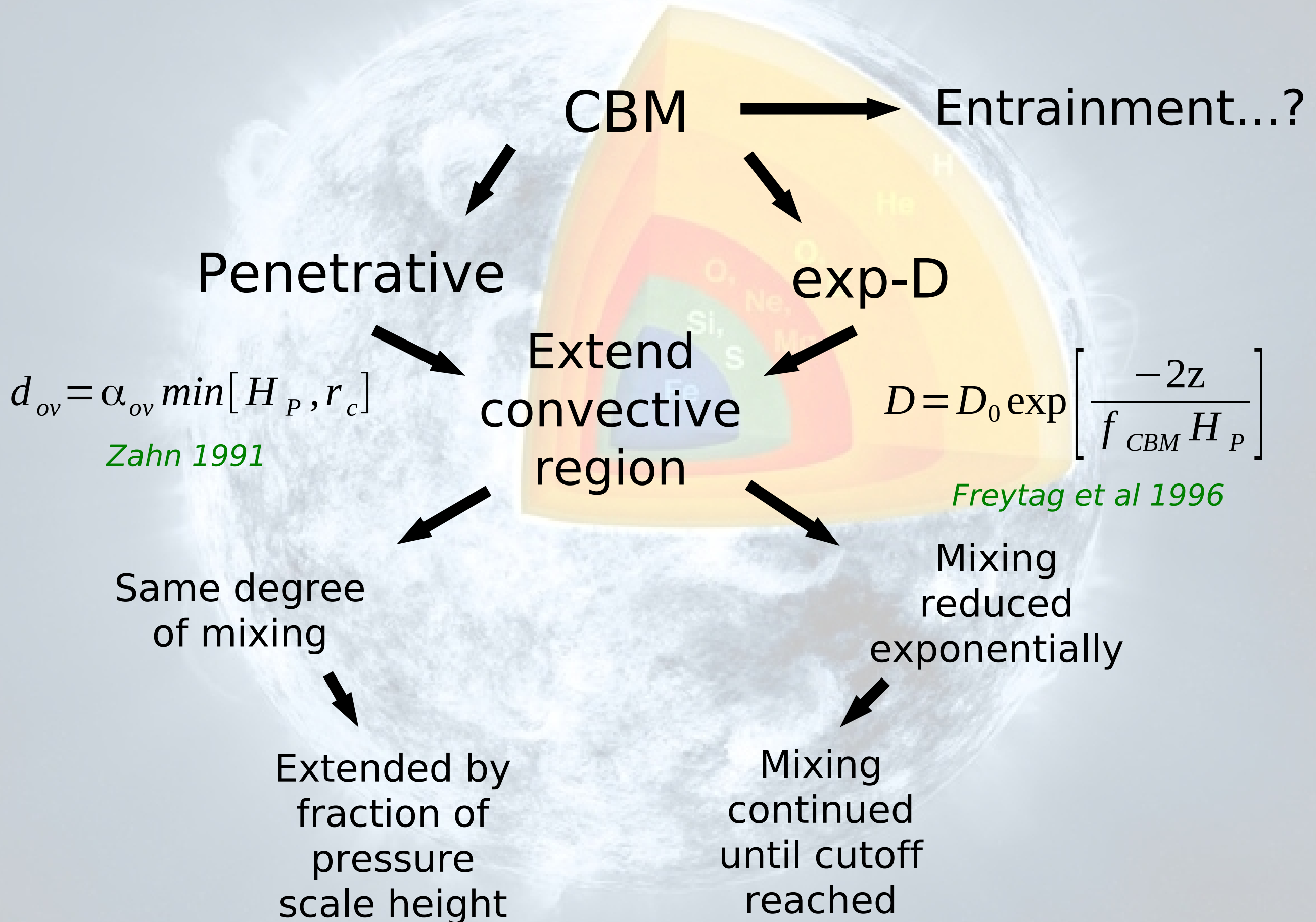
* **Carbon shell:** (PhD A. Cristini)

- + : not affected by prior shell history
- + : first stage for which thermal effects become negligible

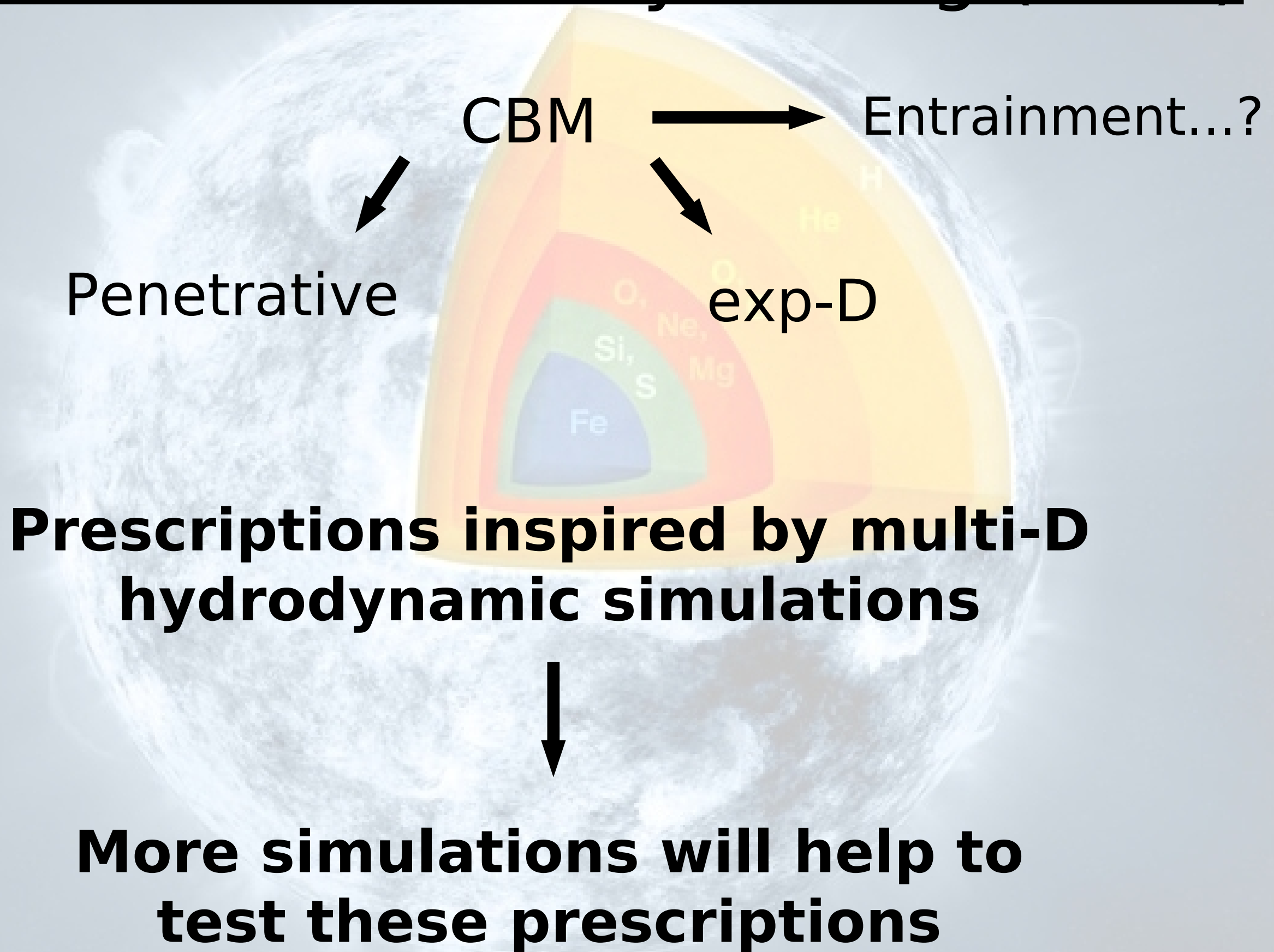
* **Envelope of RSG** (e.g. Viallet et al. [2013](#), Chiavassa et al [2009-2013](#)),



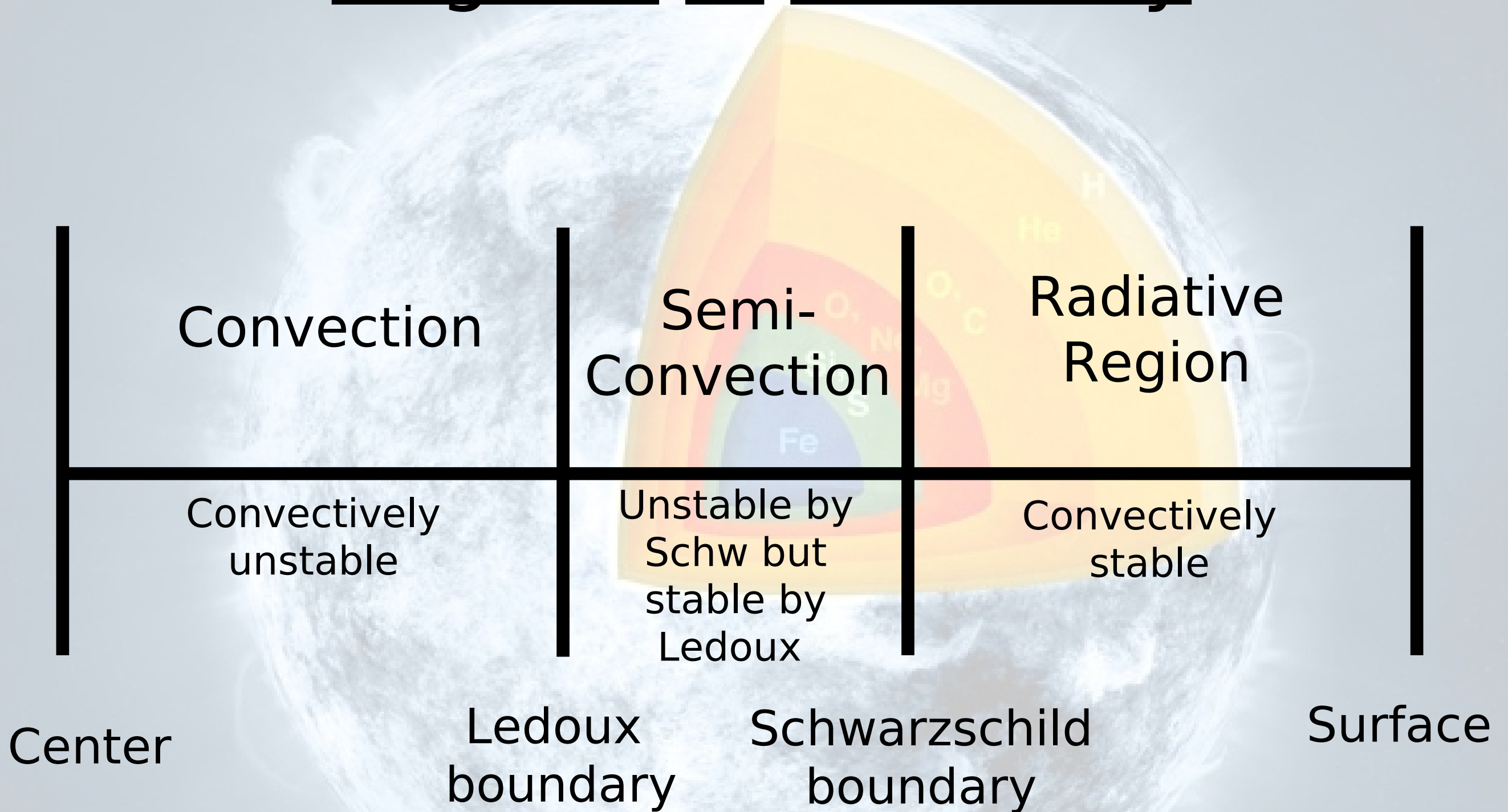
3D to 1D: Convective boundary mixing (CBM)



Convective boundary mixing (CBM)

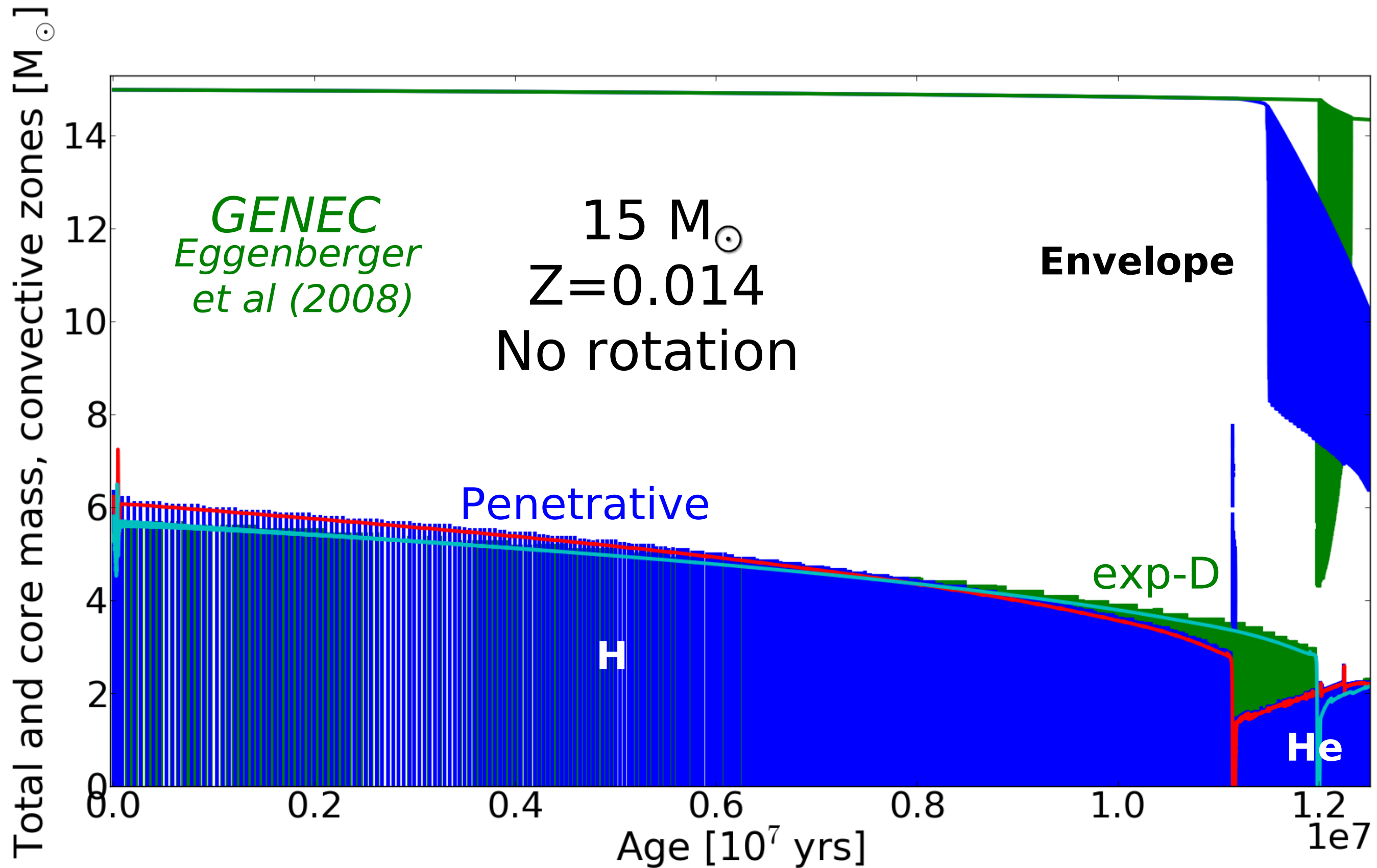


Regions of instability



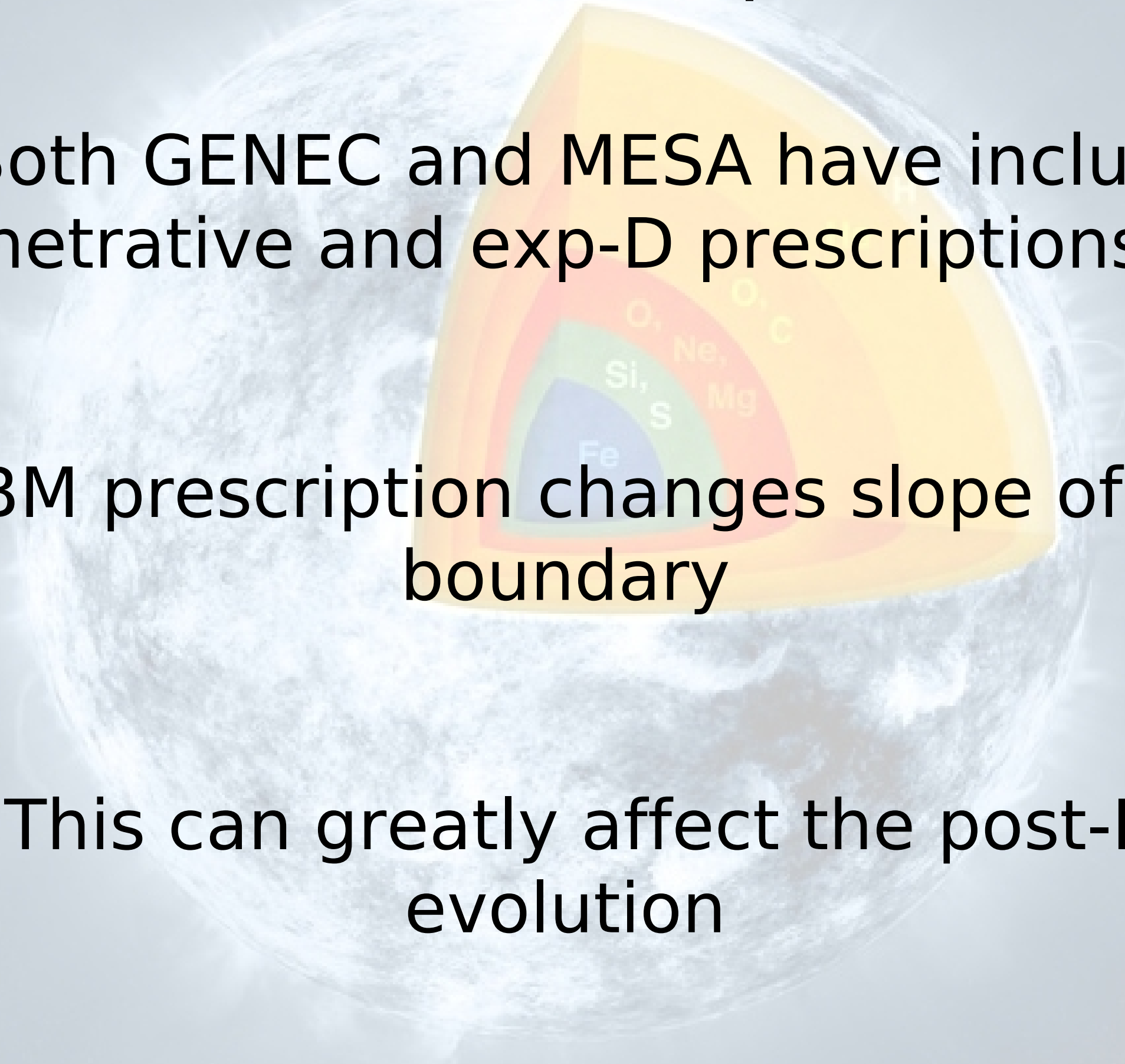
All stars $\sim > 1.8M_{\odot}$ have
this structure on MS

Penetrative vs exp-D CBM



Penetrative vs exp-D CBM

- Both GENECA and MESA have included penetrative and exp-D prescriptions.
- CBM prescription changes slope of core boundary
- This can greatly affect the post-MS evolution



Convective boundary mixing

- Convective flux and velocity zero at the boundary
- Convective boundary mixing (CBM) observed in 3D hydrodynamical simulations.

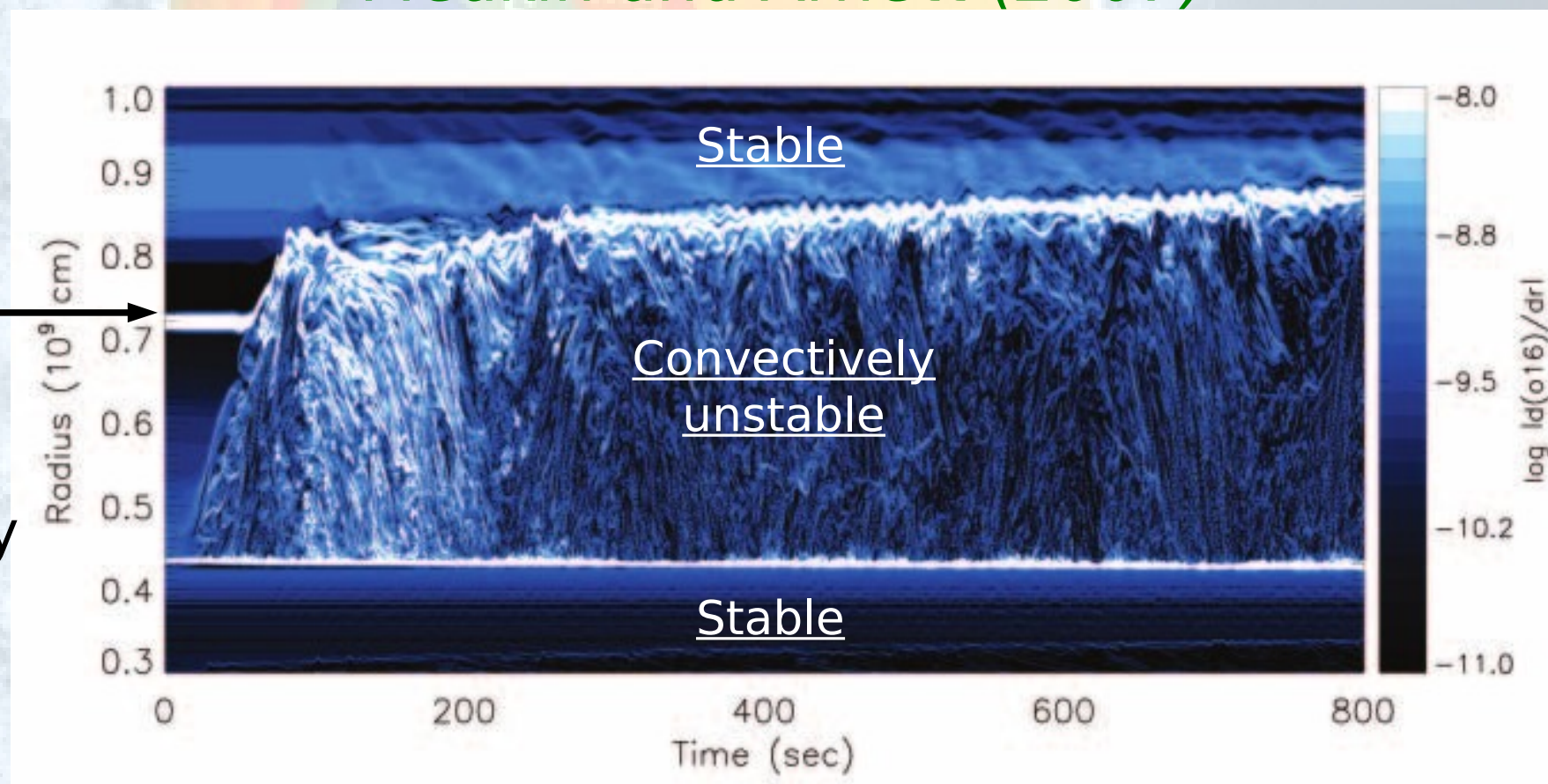
O burning shell of $23 M_{\odot}$ star simulated using PROMPT

Mass
entrainment
beyond
boundary

New processes
needed in 1D to
capture CBM

Ledoux
boundary

Meakin and Arnett (2007)

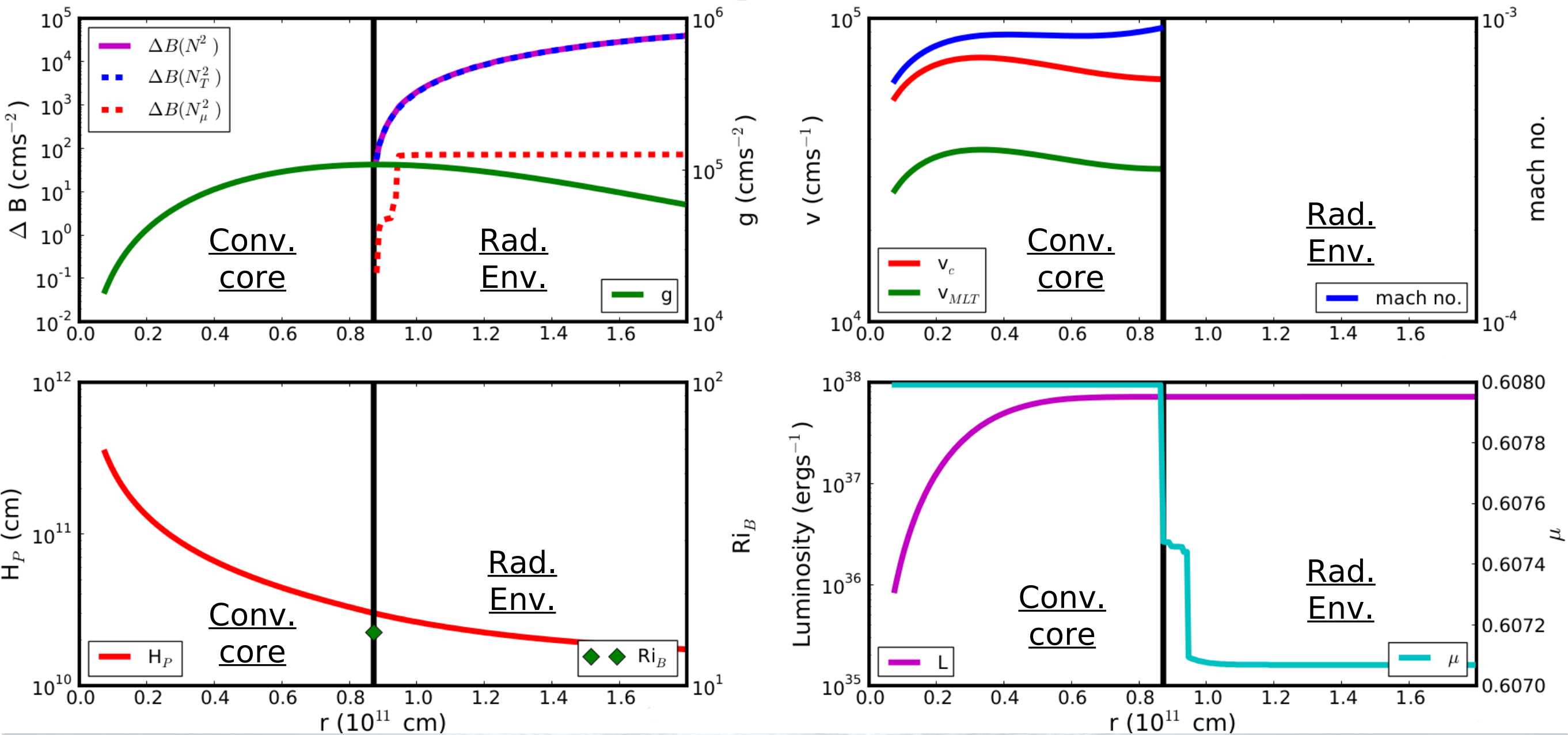


*See also e.g.
Woodward, Herwig et al 2013*

Due to free parameters in MLT and CBM in 1D
further multi-D simulations needed to
understand CBM

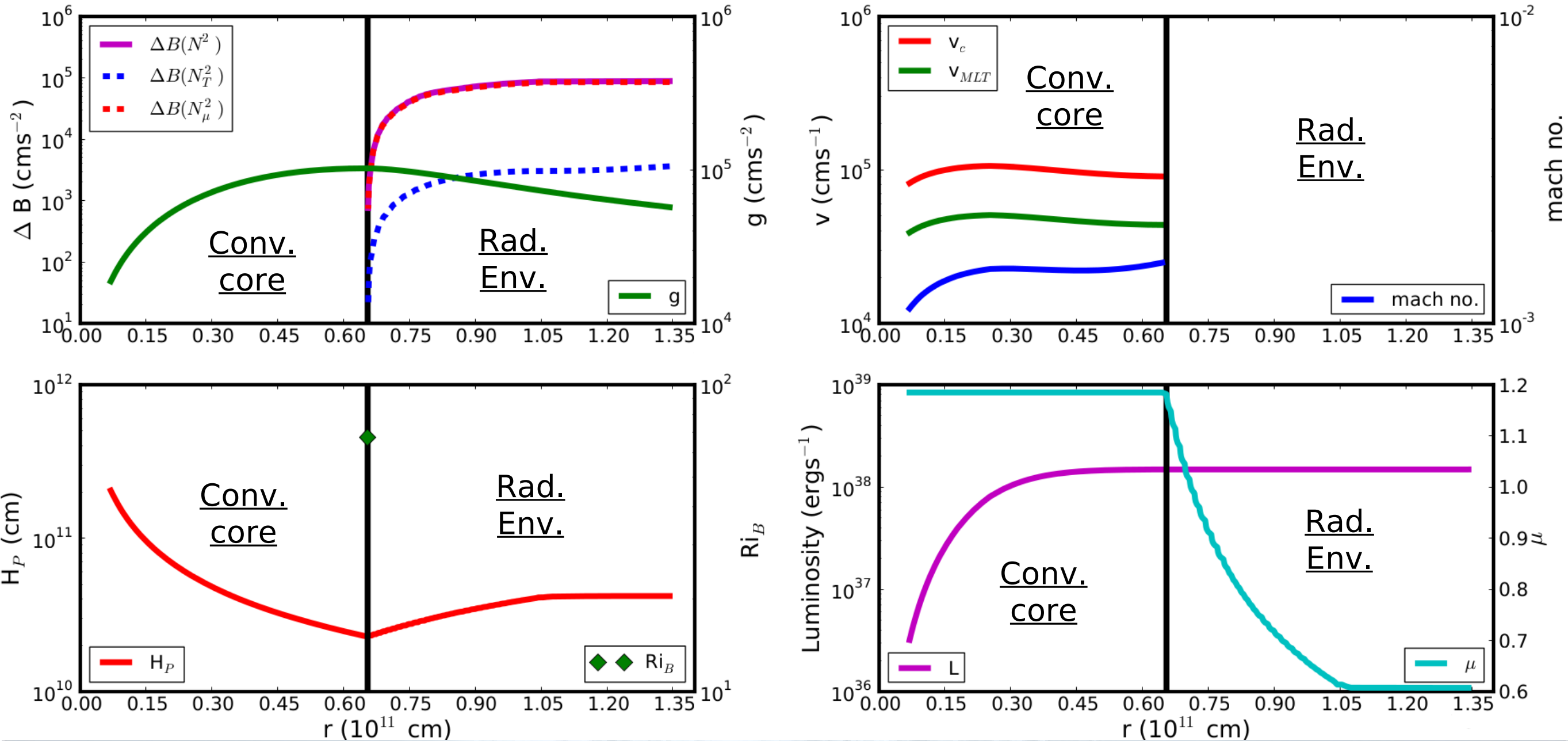
Burning zones

Core H burning (0.3% fuel burnt)



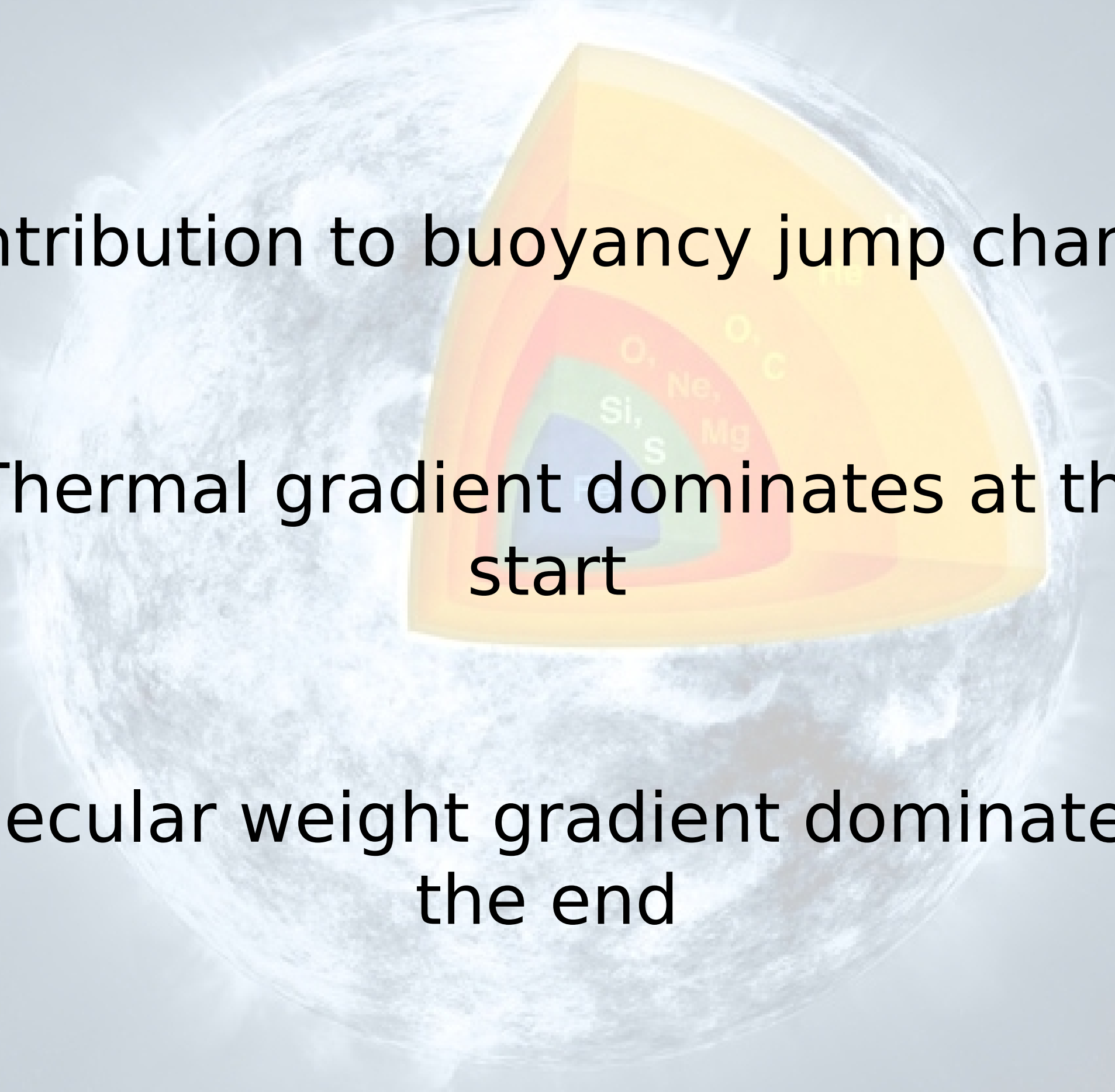
Burning zones

Core H burning (90.5% fuel burnt)

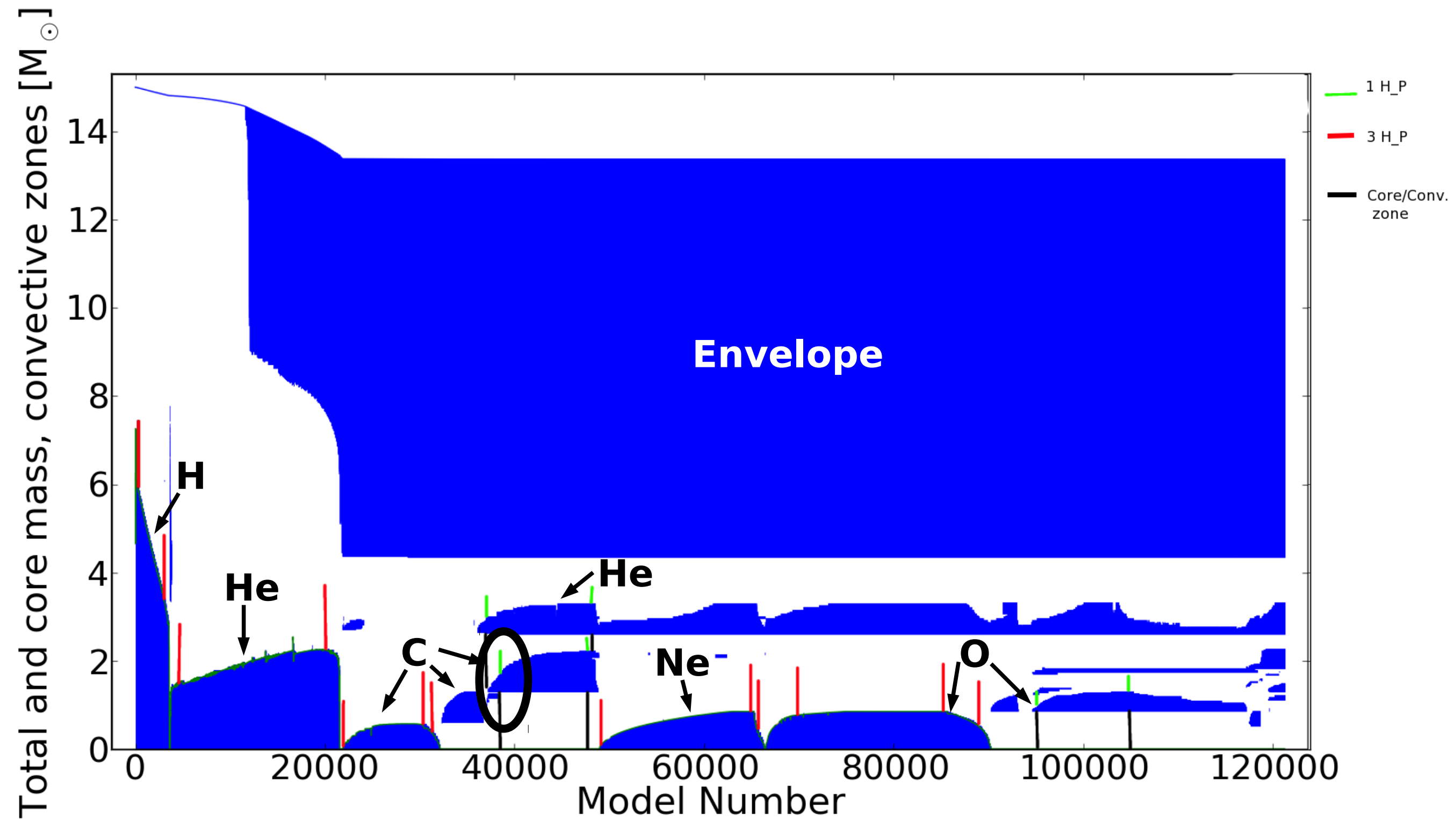


Remarks

- Contribution to buoyancy jump changes
- Thermal gradient dominates at the start
- Molecular weight gradient dominates at the end

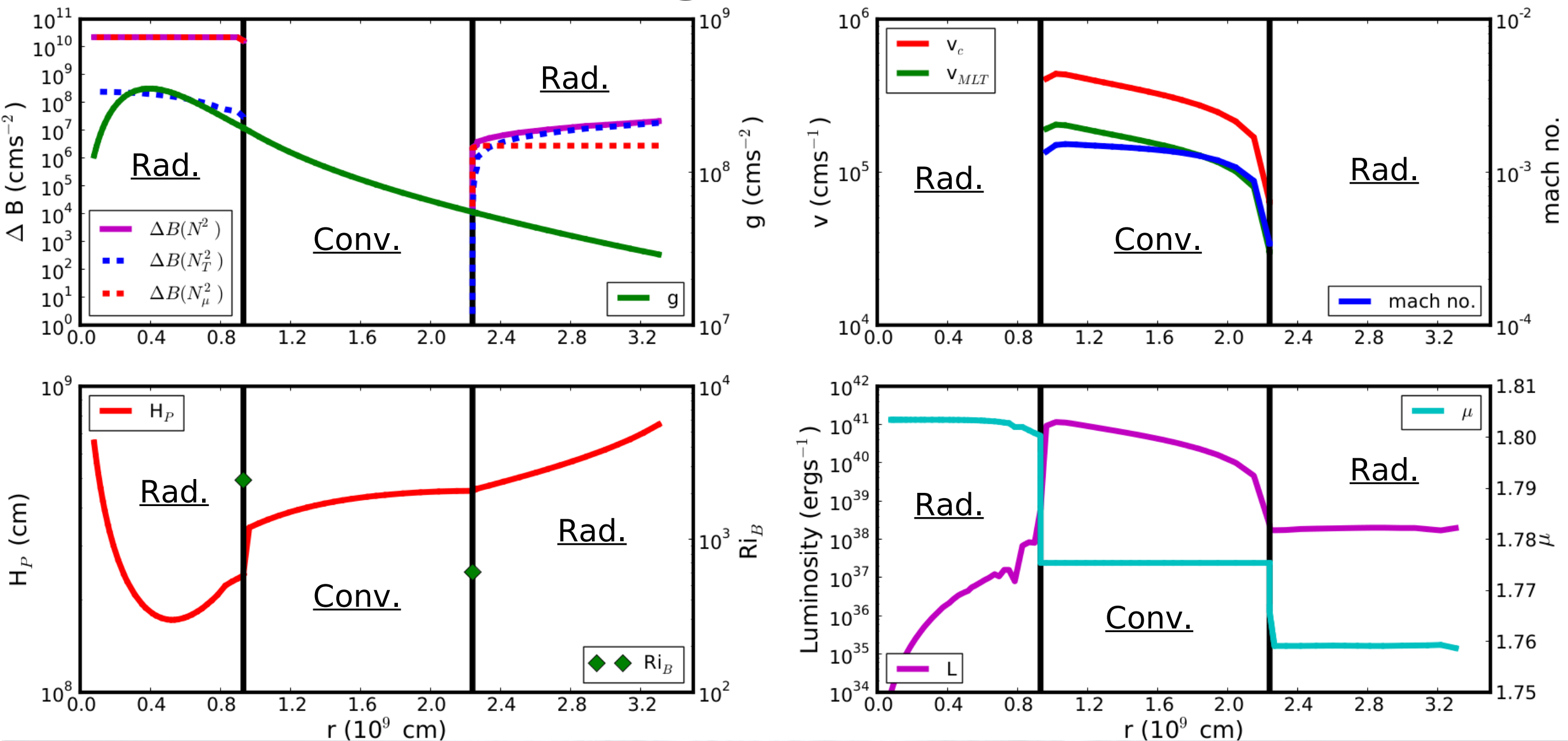


Burning zones



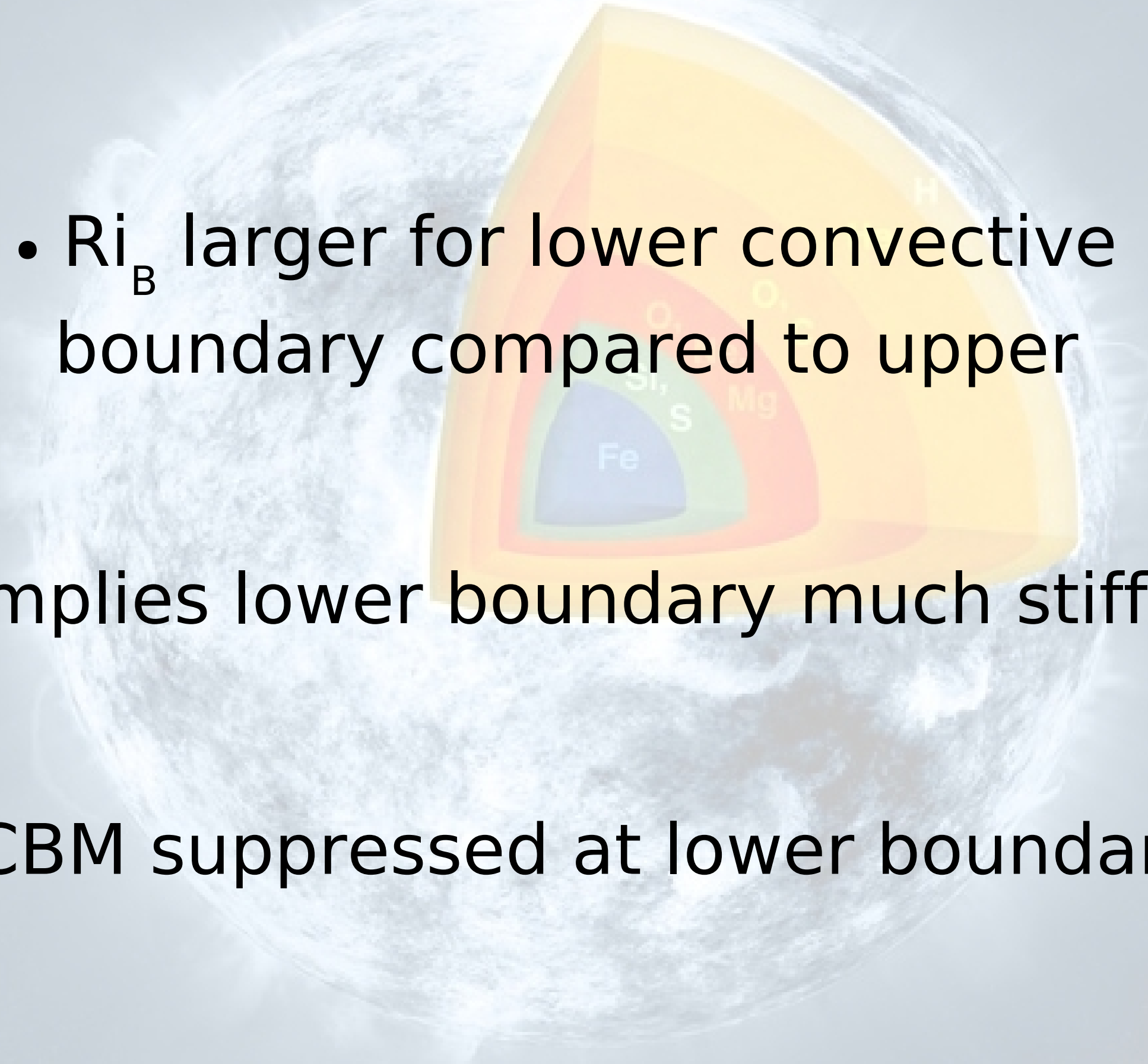
Burning zones

Shell C burning (31% of shell lifetime)



Remarks

- Ri_B larger for lower convective boundary compared to upper
- Implies lower boundary much stiffer
- CBM suppressed at lower boundary



Conclusions thus far

- exp-D CBM changes slope of core boundary
- Thermal and μ gradients dominate buoyancy jump at the start and end of MS, respectively
- Lower boundary of convective shells are stiffer than upper boundaries

1D to 3D: Key Uncertainties

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 - -: difficult to model due to important radiative effects
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- Silicon burning:
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 -
 - Carbon shell: (Cristini et al in prep)
 - +: not affected by prior shell history
 - Envelope convection for RSG, low-mass stars, ... ?