



# EoS and compact objects : status quo and open problems

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Brainstorming on  
Compact objects, their equation of state,  
related explosive events, and their nucleosynthesis  
Basel, 29 Sept-1 Oct, 2016

# Phenomenological vs. ab initio approaches

## Phenomenological approaches

Based on effective density-dependent NN force with parameters fitted on nuclei properties.

- **Liquid Drop models**
  - ✧ BPS Baym et al, *ApJ* **170**, 299 (1971)
  - ✧ BBP Baym et al., *NPA* **175**, 225 (1971)
  - ✧ LS Lattimer&Swesty, *NPA* **535**, 331 (1991)
  - ✧ DH Douchin&Haensel, *A&A* **380**, 151 (2001)
- **TF + RMF**
  - ✧ Shen et al., *NPA* **637**, 435 (1998)
- **ETFSI + Eff. Skyrme force**
  - ✧ BSk Goriely et al., *PRC* **82**, 035804 (2010)
- **Hartree-Fock**
  - ✧ NV Negele&Vautherin, *NPA* **207**, 298 (1973)
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  - ✧ RHF Boussy et al., *PRL* **55**, 1731 (1985)
  - ✧ QMC Guichon et al., *NPA* **814**, 66 (2008)
- **Statistical models**
  - ✧ NSE Raduta&Gulminelli. *PRC* **82**, 065801 (2010)
  - ✧ HS Hempel&Schaffner-Bielich, *NPA* **837**, 210 (2010)

## Ab initio approaches

The nuclear problem is solved starting from the two- and three-body realistic nucleon interaction.

- **Diagrammatic**
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  - ✧ SCGF Kadanoff&Baym, *Quantum Statistical Mechanics* (1962)
  - ✧ DBHF Ter Haar&Malfiet, *Phys. Rep.* **149**, 207 (1987);
- **Variational**
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  - ✧ FHNC Fantoni&Rosati, *Nuovo Cimento A* **20**, 179 (1974)
  - ✧ CBF Fabrocini&Fantoni, *PLB* **298**, 263(1993)
  - ✧ LOCV Owen et al., *NPA* **277**, 45 (1978)
- **Monte Carlo**
  - ✧ VMC Wiringa, *PRC* **43**, 1585 (1991)
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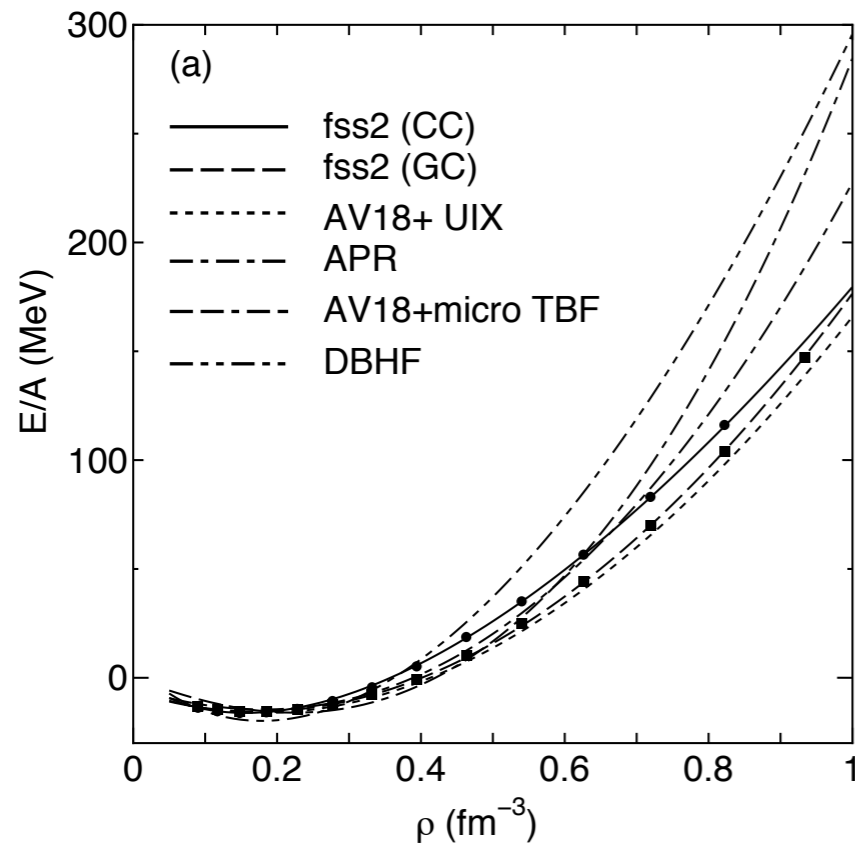
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A comparison among the different approaches :  
NM saturation point and TBF's

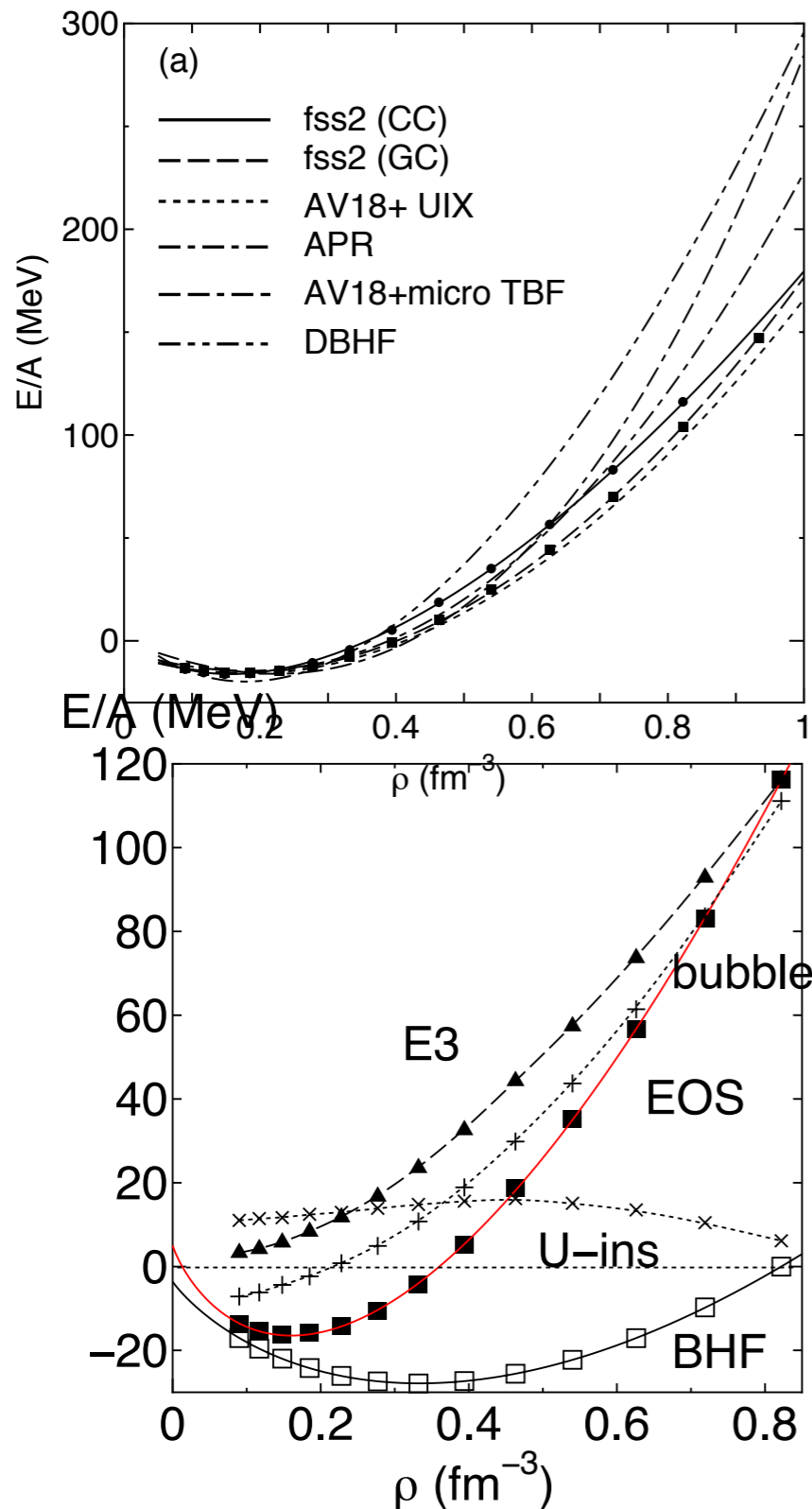
# A comparison among the different approaches : NM saturation point and TBF's



BBG (AV18+micro TBF, AV18 + UIX, fss2)

- \* Microscopic vs. Phenomenological TBF's.  
Saturation point well fitted. Different density dependence at large density.
- \* fss2 built from quark degrees of freedom.  
Nucleons described as three-quarks clusters with confinement. NN potential from gluon and meson exchange between quarks.  
Fujiwara et al., PRC65,014002 (2001).

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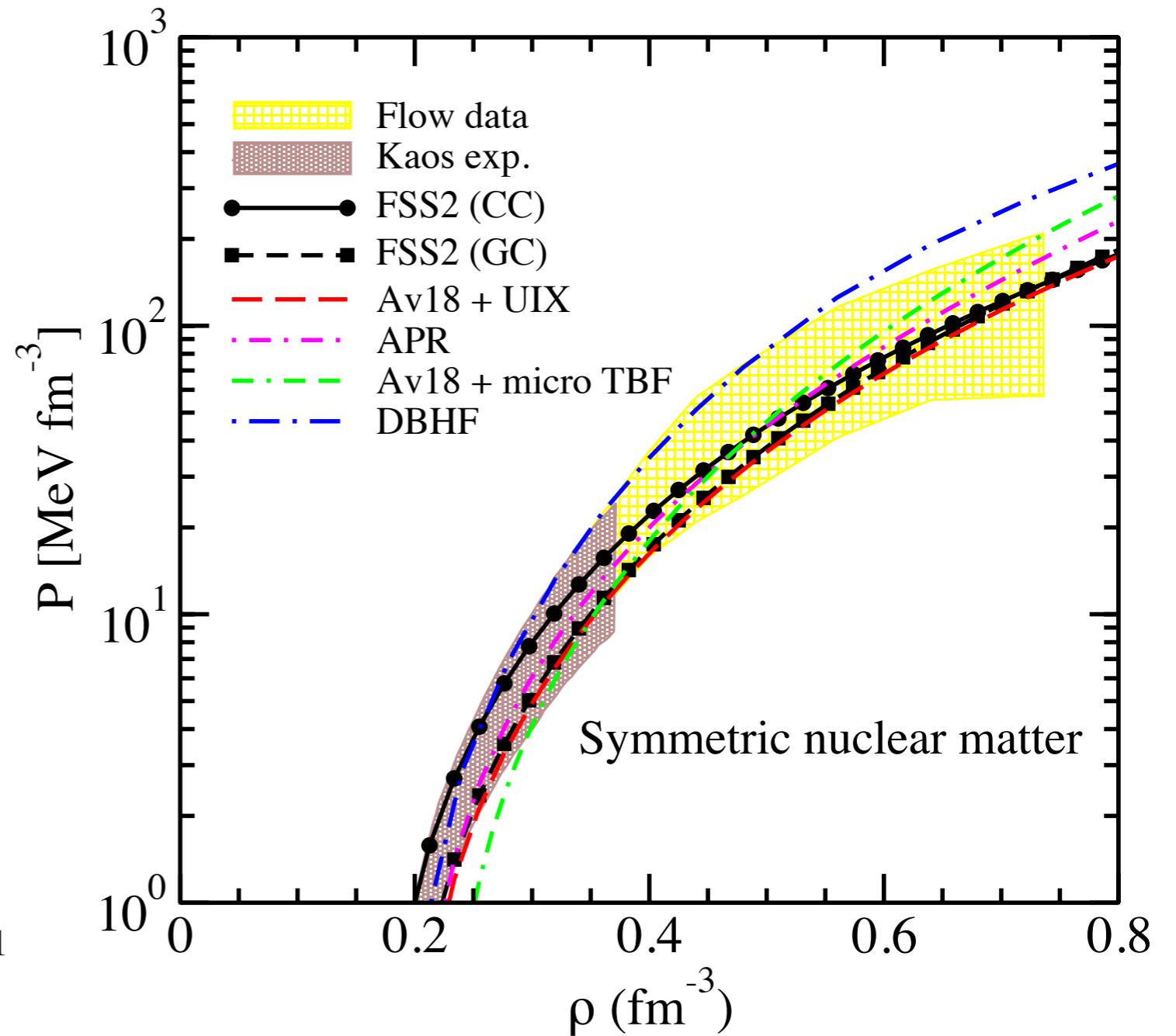
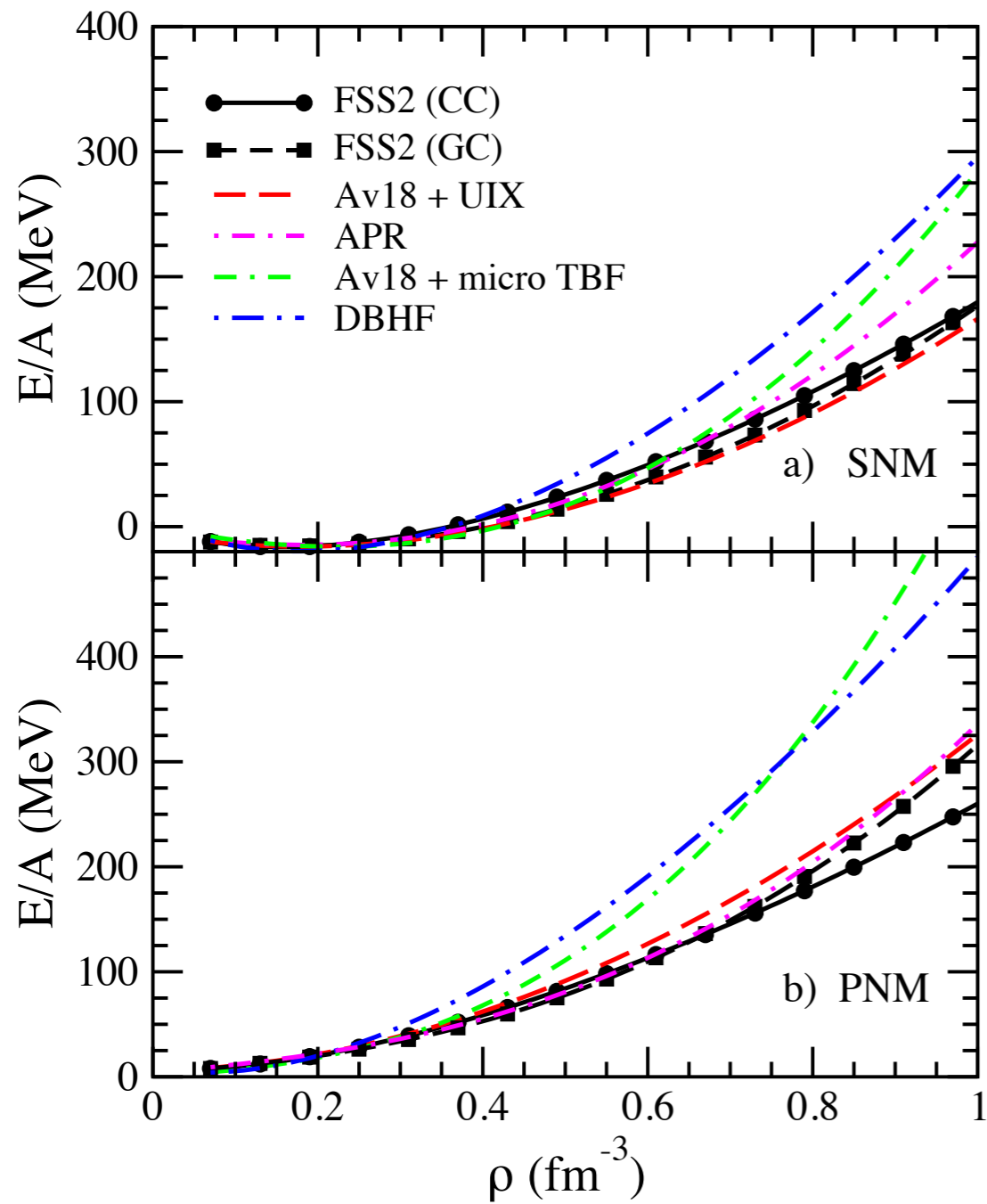


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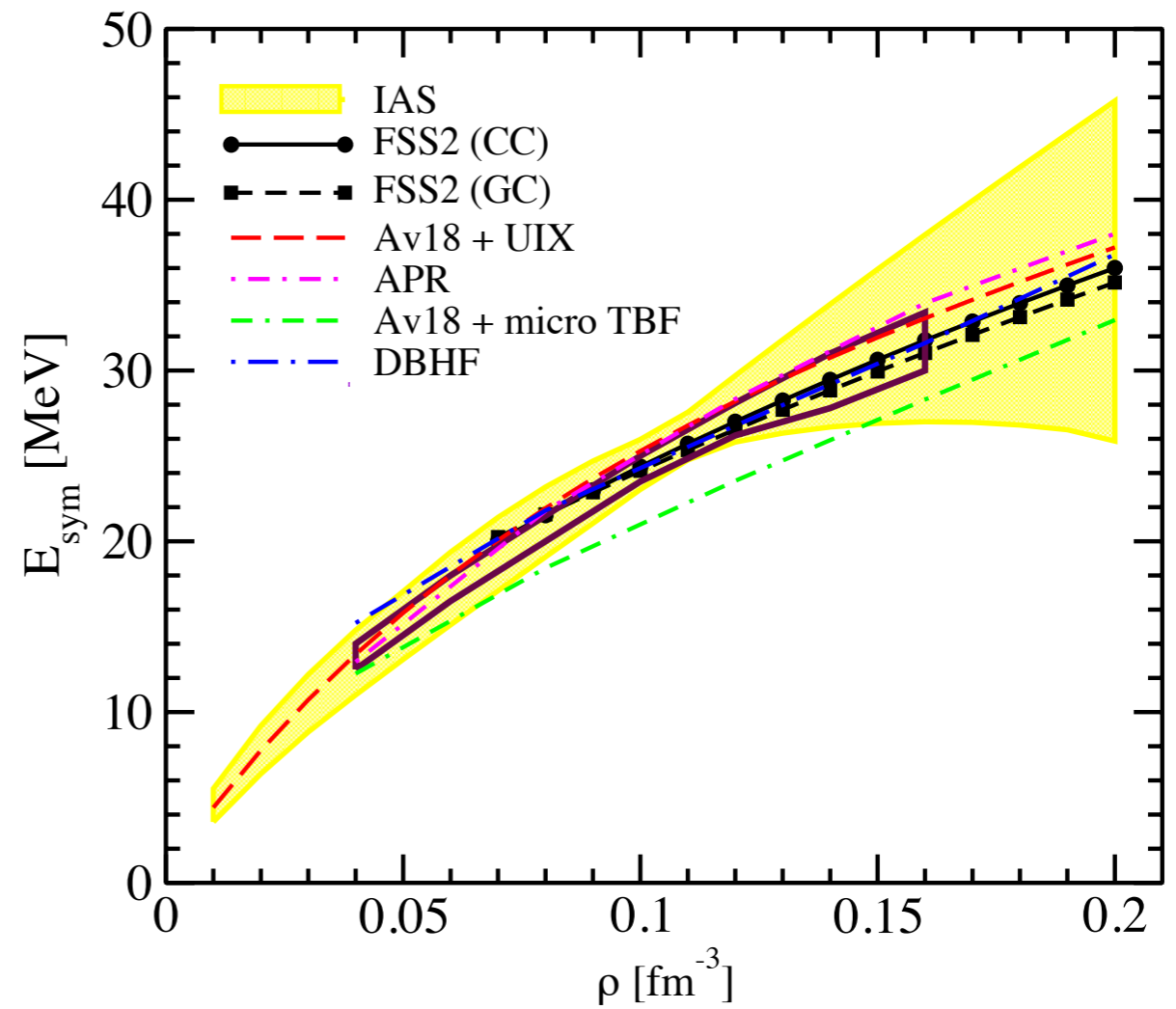
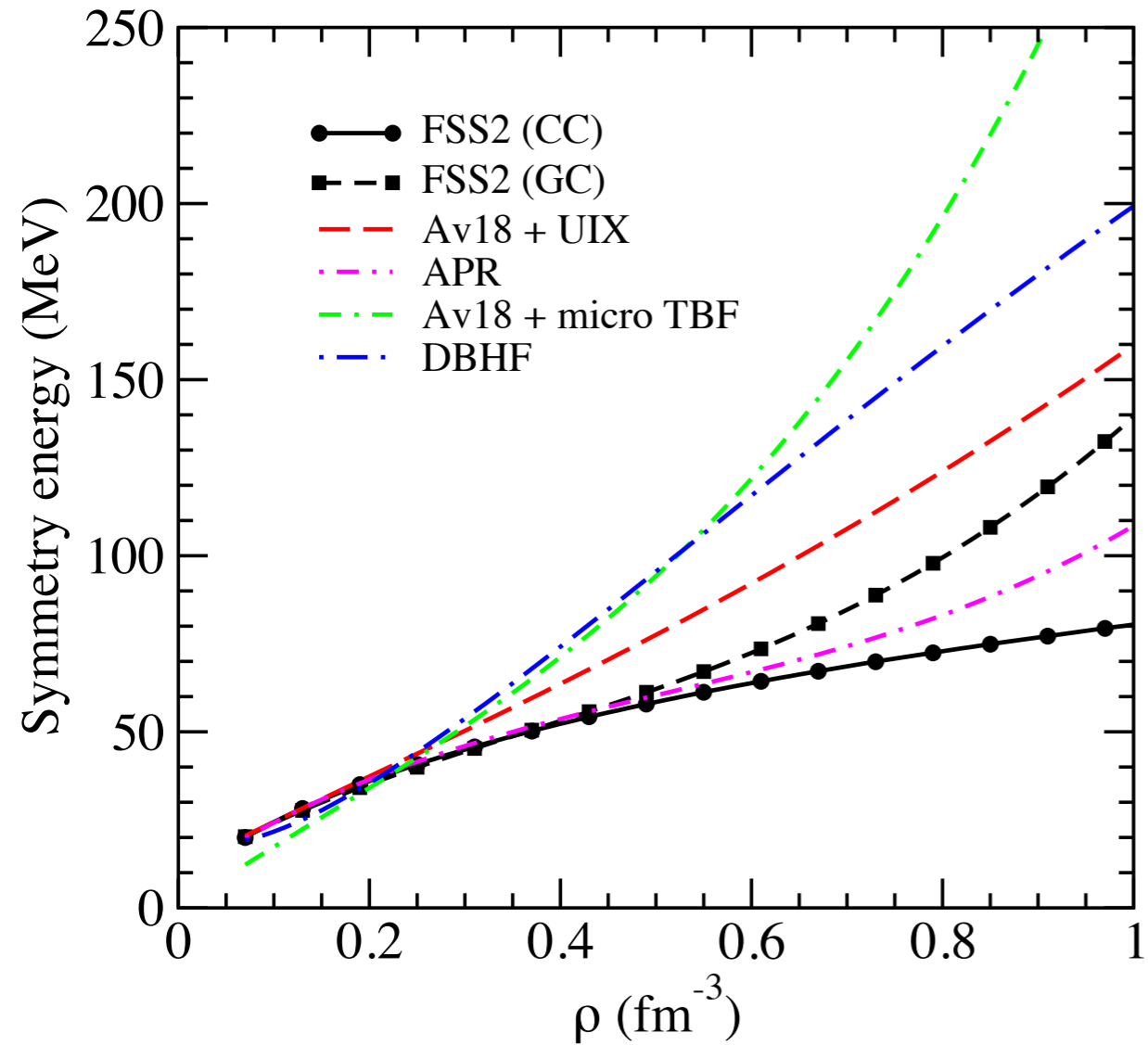
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In **fss2** the three hole-line contribution is relevant and produces a substantial saturation effect. No need of TBF's ....

# A comparison with HIC data

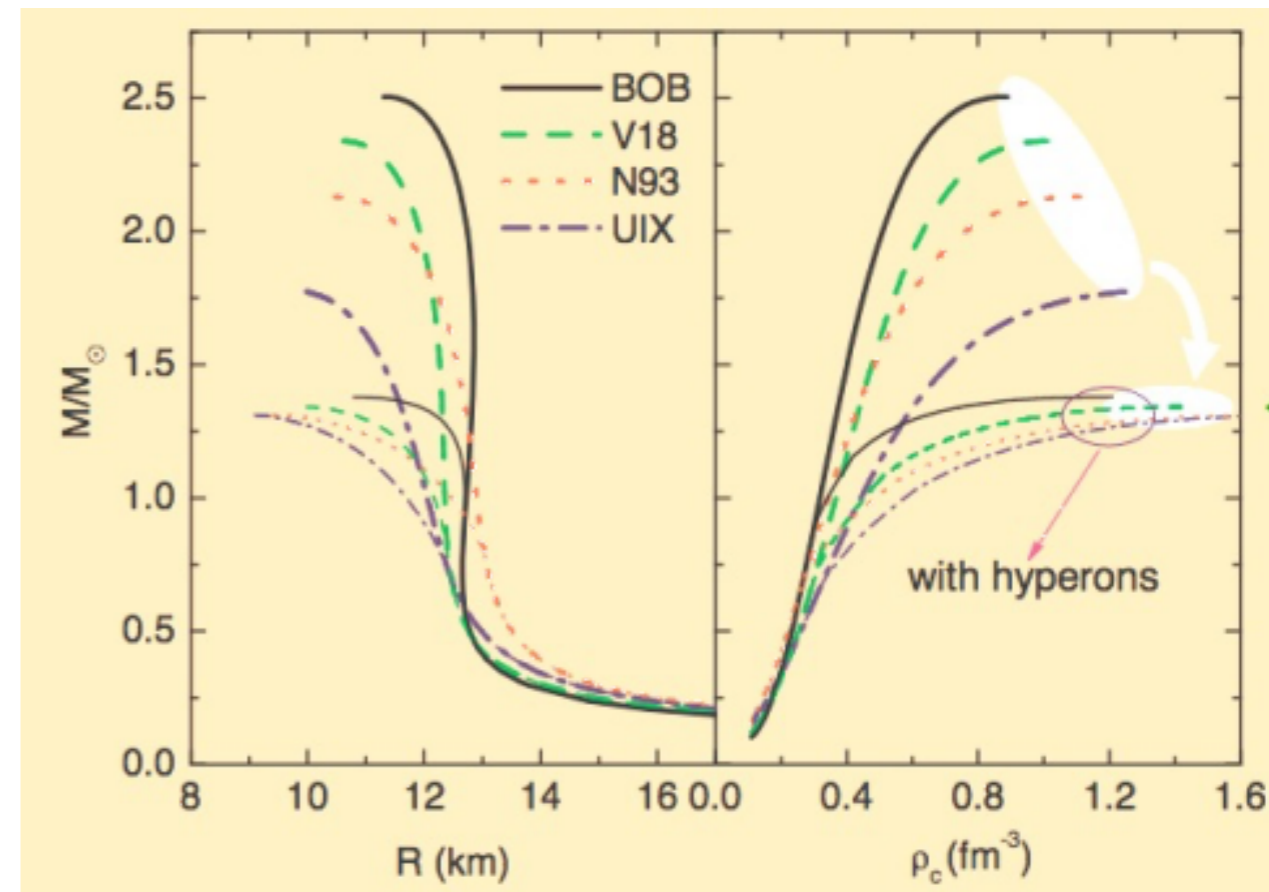
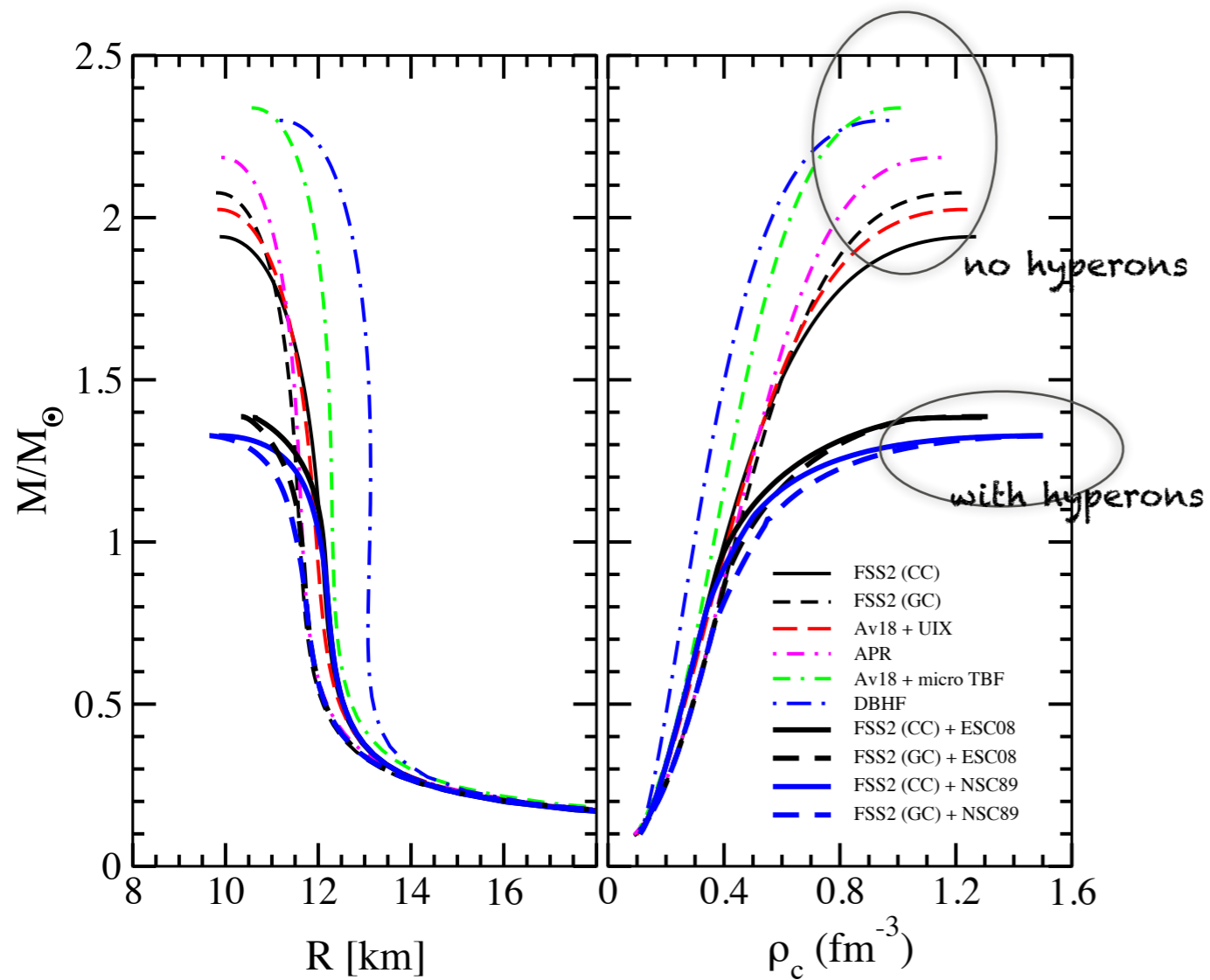


# Symmetry energy





# NS structure



The "Hyperon puzzle":  
Self-regulating softening due to  
hyperon appearance

Additional repulsion required!

# Quark matter in NS

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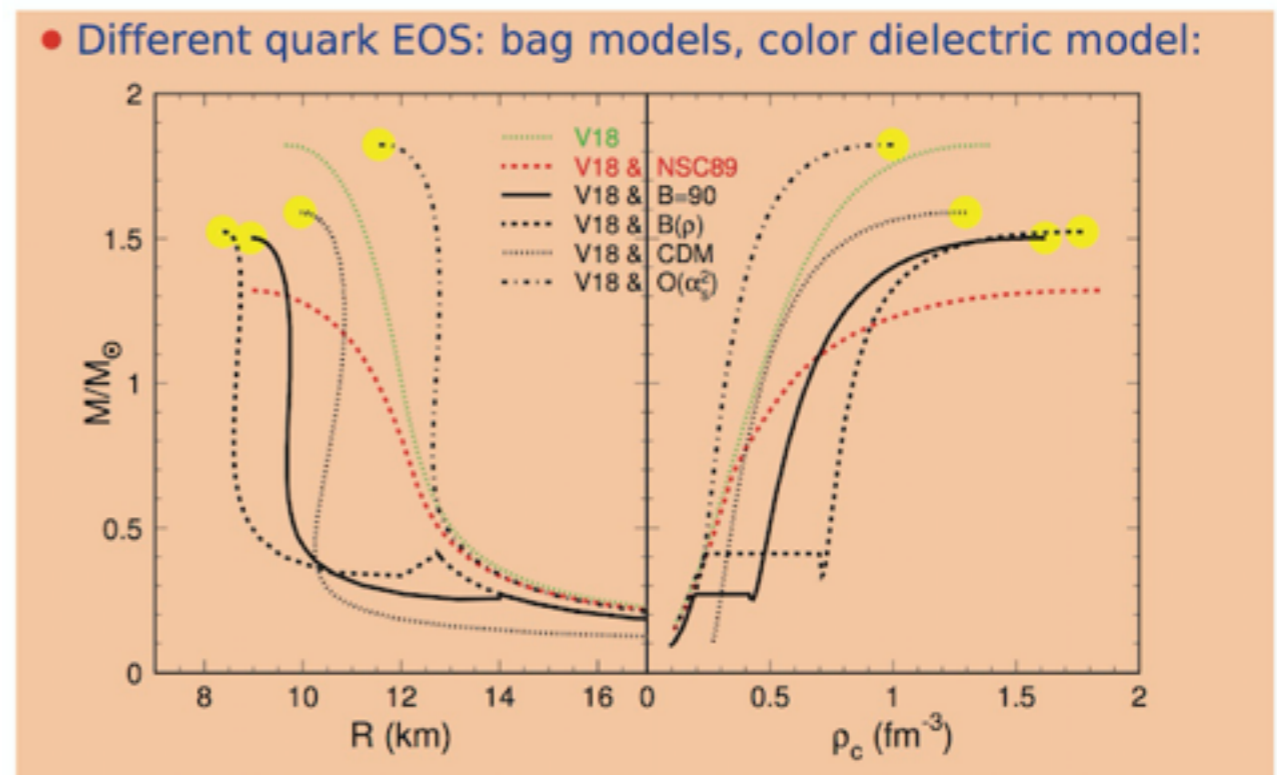
## Several models of Quark Matter

- \* MIT bag model
- \* Nambu-Jona-Lasinio model
- \* Color Dielectric model
- \* Dyson-Schwinger model
- \* Field Correlator Method model
- \* perturbative QCD model

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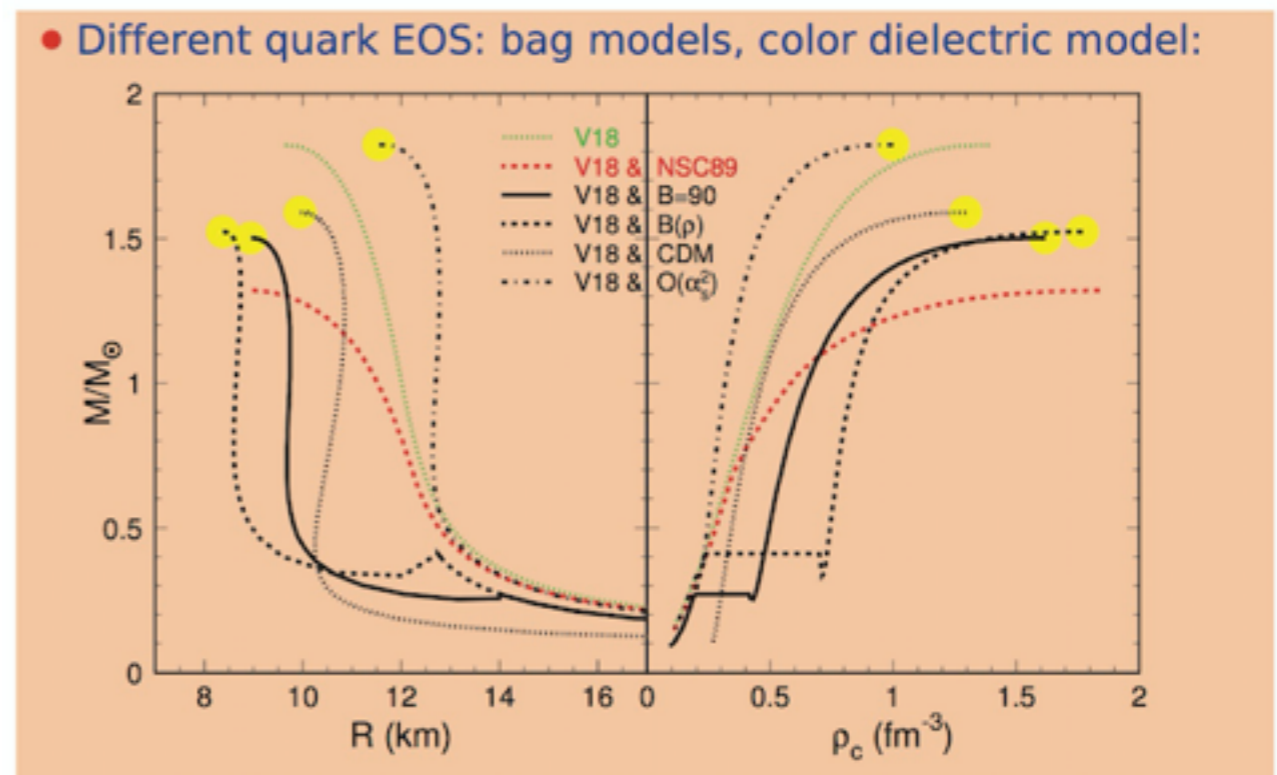
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- \* When hyperons are present in the HP (MIT, pQCD, FCM), the limiting mass stays below  $2 M_{\odot}$ . maximum masses :  $1.5 \dots 1.9 M_{\odot}$  with different radii !
- \* With NJL, DS models hyperons prevent the phase transition and the limiting mass can be larger than  $2 M_{\odot}$ .

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fss2 potential based on quark d.o.f. does not need TBF's  
True also for other cases ? Issue to be explored ...

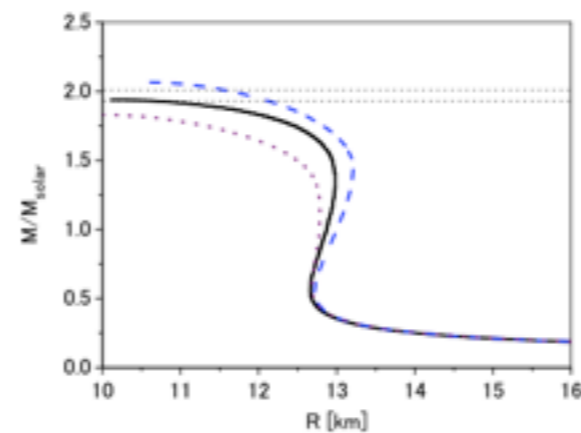
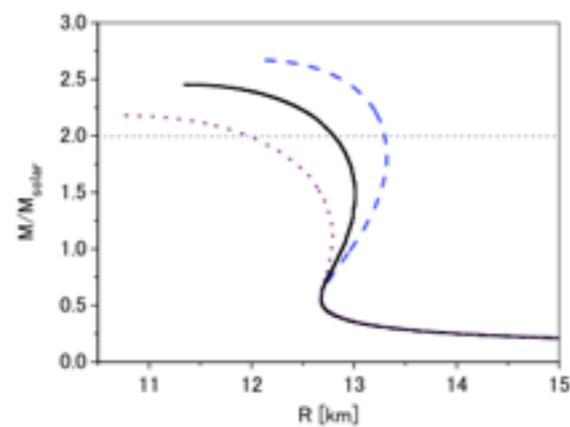
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EOS based on multi-pomeron potential





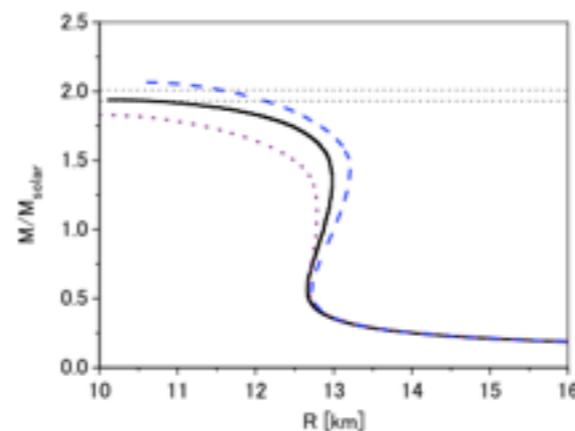
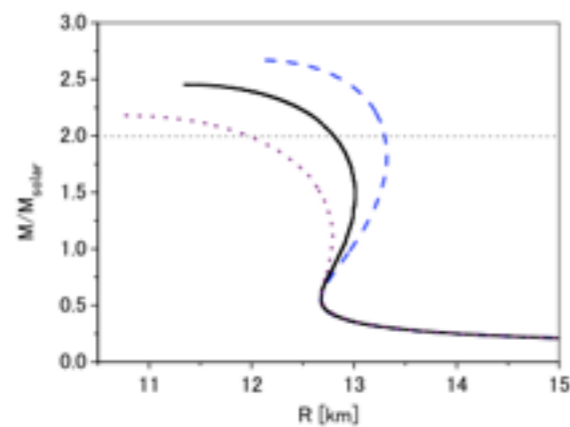
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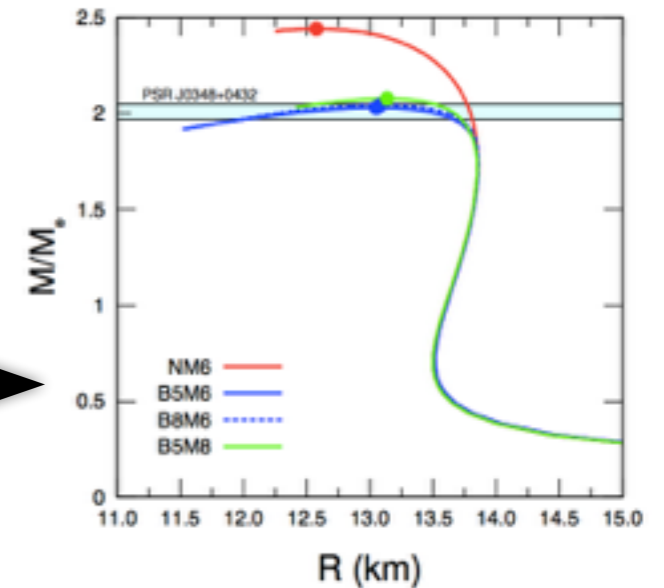
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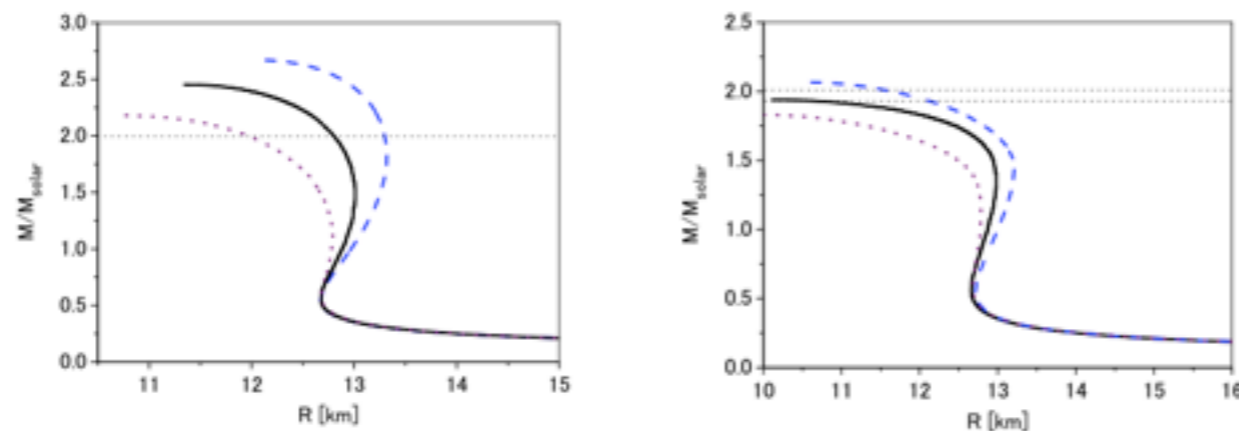
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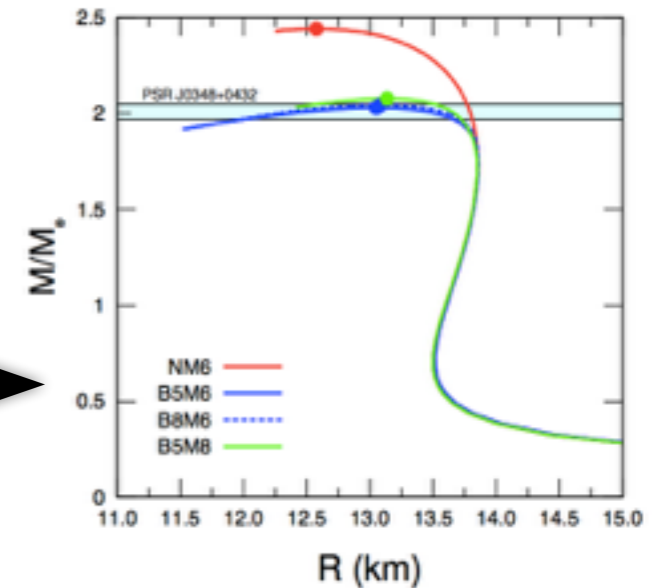
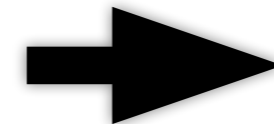
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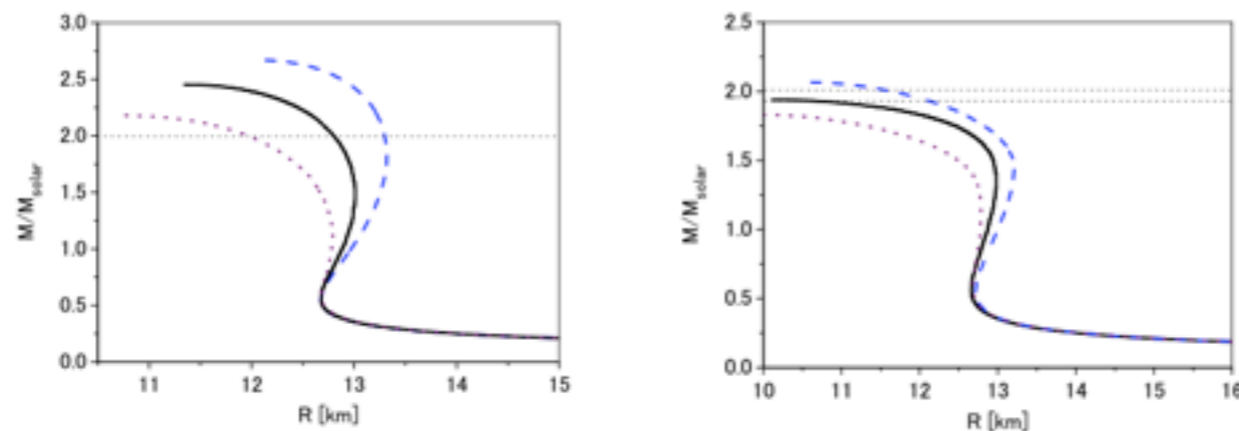
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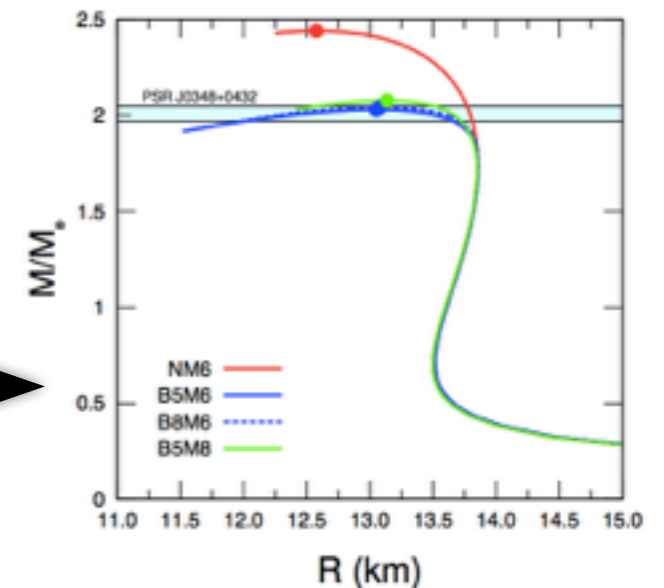
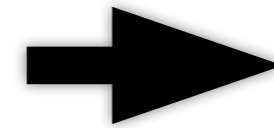
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Issue IV : EOS at finite T,  $T > T_F$